



# Characterization of the internal structure snow and ice packs using 3-D SAR imaging at various scales

**Laurent Ferro-Famil <sup>(1)</sup> & Stefano Tebaldini <sup>(2)</sup>**

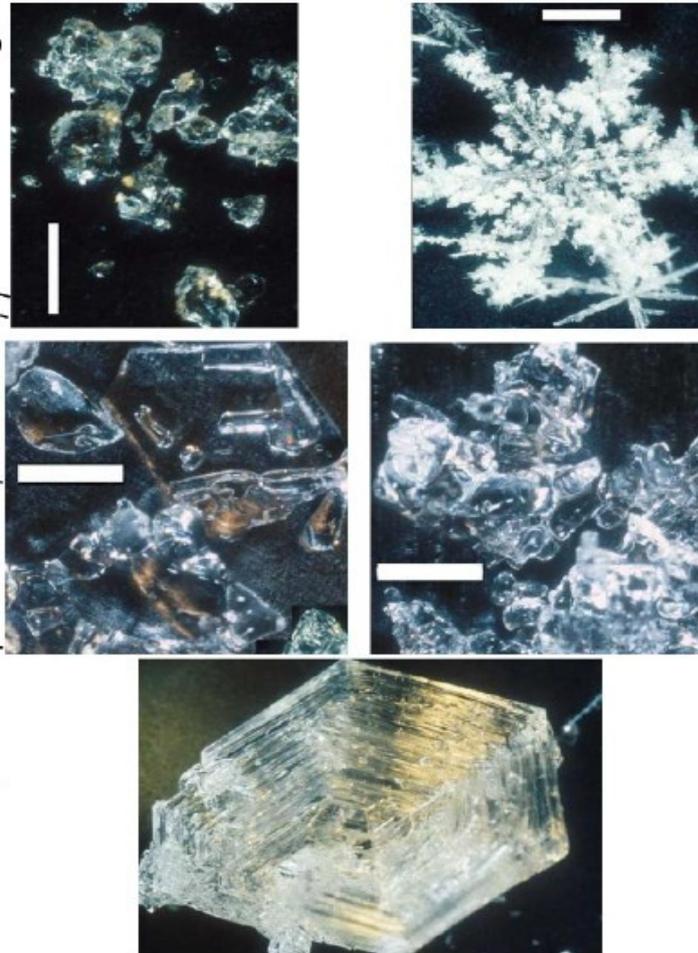
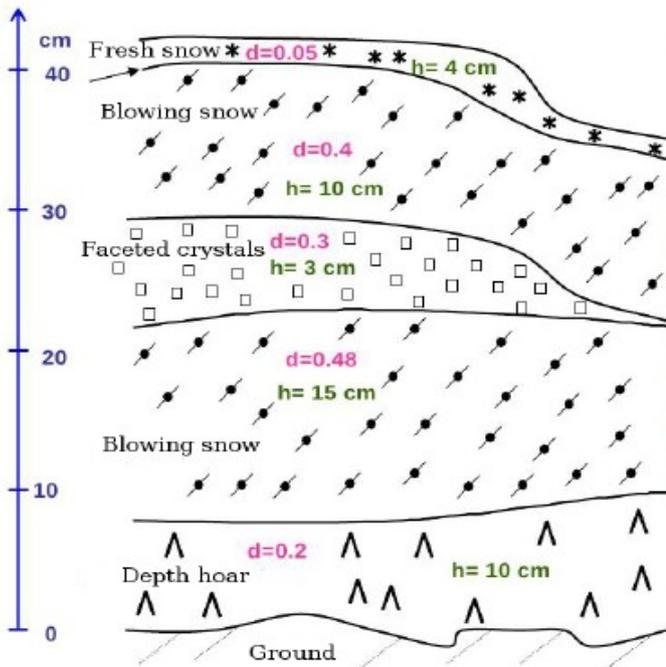
**(1) IETR, University of Rennes 1, France**

**(2) DEIB, Politecnico di Milano, Italy**

`Laurent.Ferro-Famil@univ-rennes1.fr`



Sample of snowpack in the Arctic (F. Domine et al.)  
82°30'N, 62°20'W

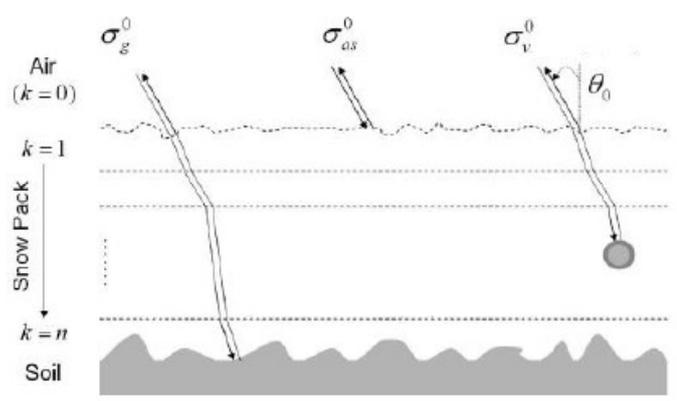
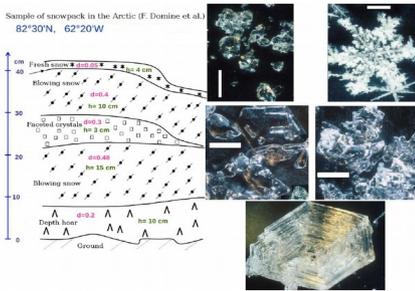


## Snowpack:

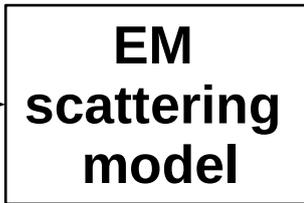
- dense and complex medium, made of several layers
- 1 layer  $\equiv$  several parameters: thickness, grain size, density, liquid water content ...
- Spatial and temporal variations



Sample of snowpack in the Arctic (F. Domino et al.)  
82°30'N, 62°20'W



Physical parameters  
(tens:  $N \times 10$ )



Modeled  
scattering coefficients  
( $\ll 10$ )

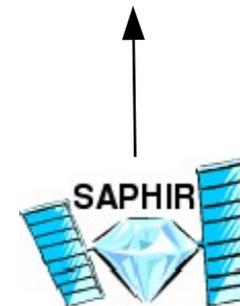
Estimated  
physical parameters  
(tens:  $N \times 10$ )



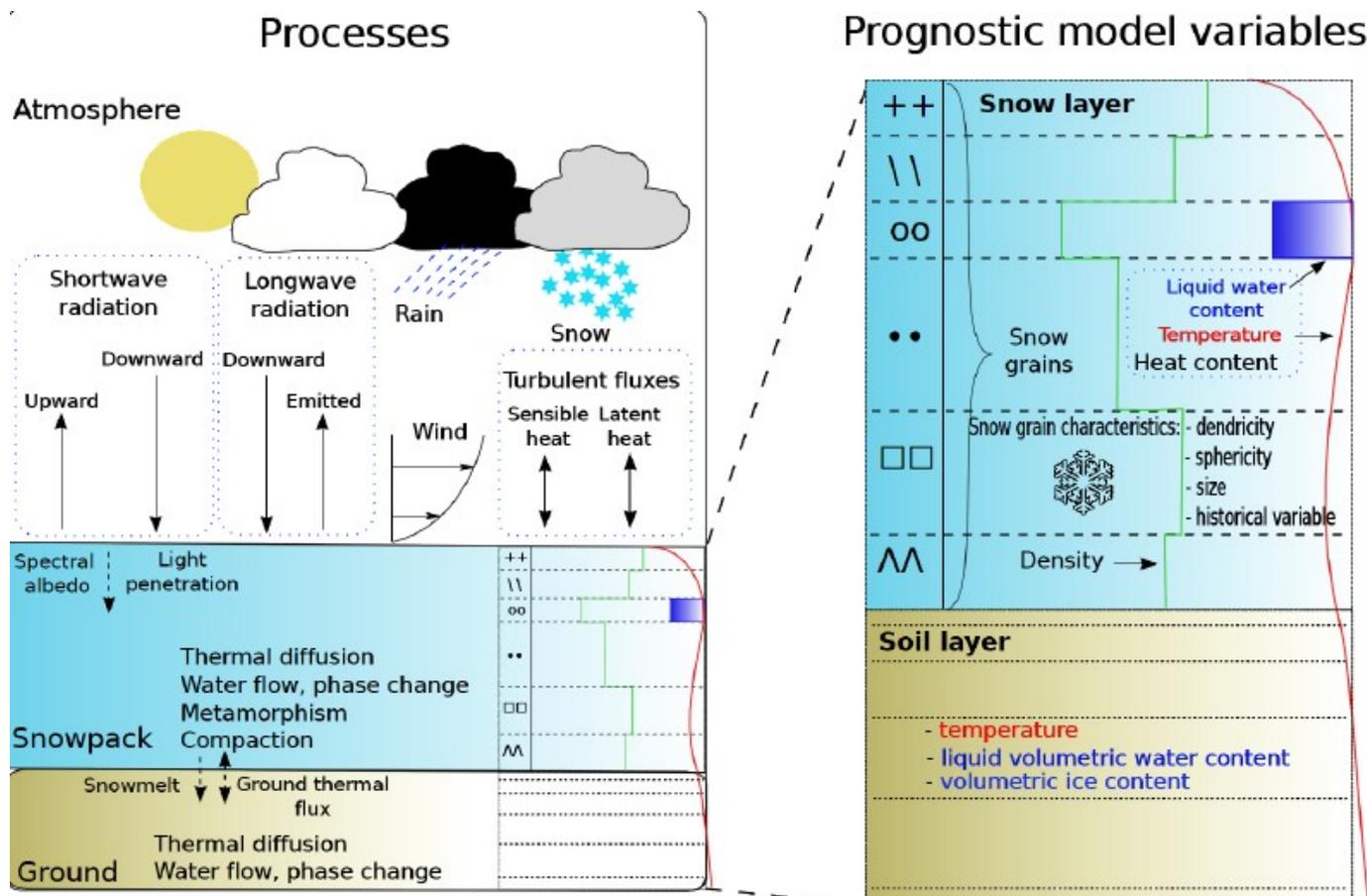
Measured  
scattering coefficients  
( $\ll 10$ )

Snowpack structure estimation from SAR data

Guess tens of parameters from a few measurements  
⇒ Highly badly conditioned inverse problem

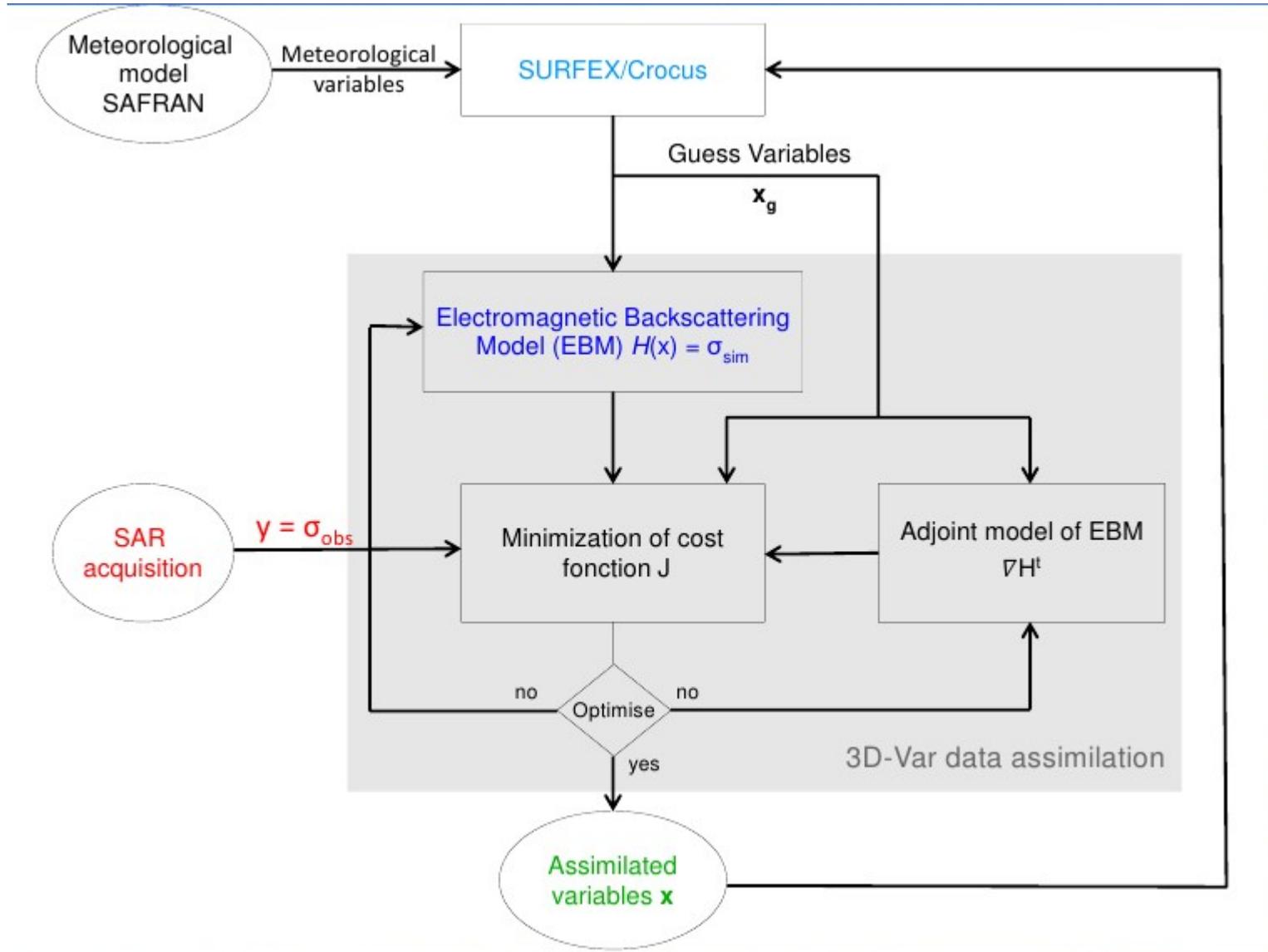


**Need for additional information !**



- MeteoFrance meteorological model simulating the structure of snowpacks
- 1D snowpack temporal evolution model
- Operates without in-situ measurements (open loop), no in-situ measurements
- Very low spatial resolution

**Provides a stable initial guess of the snowpack structure  
 ⇒ inverse problem conditioning improvement**

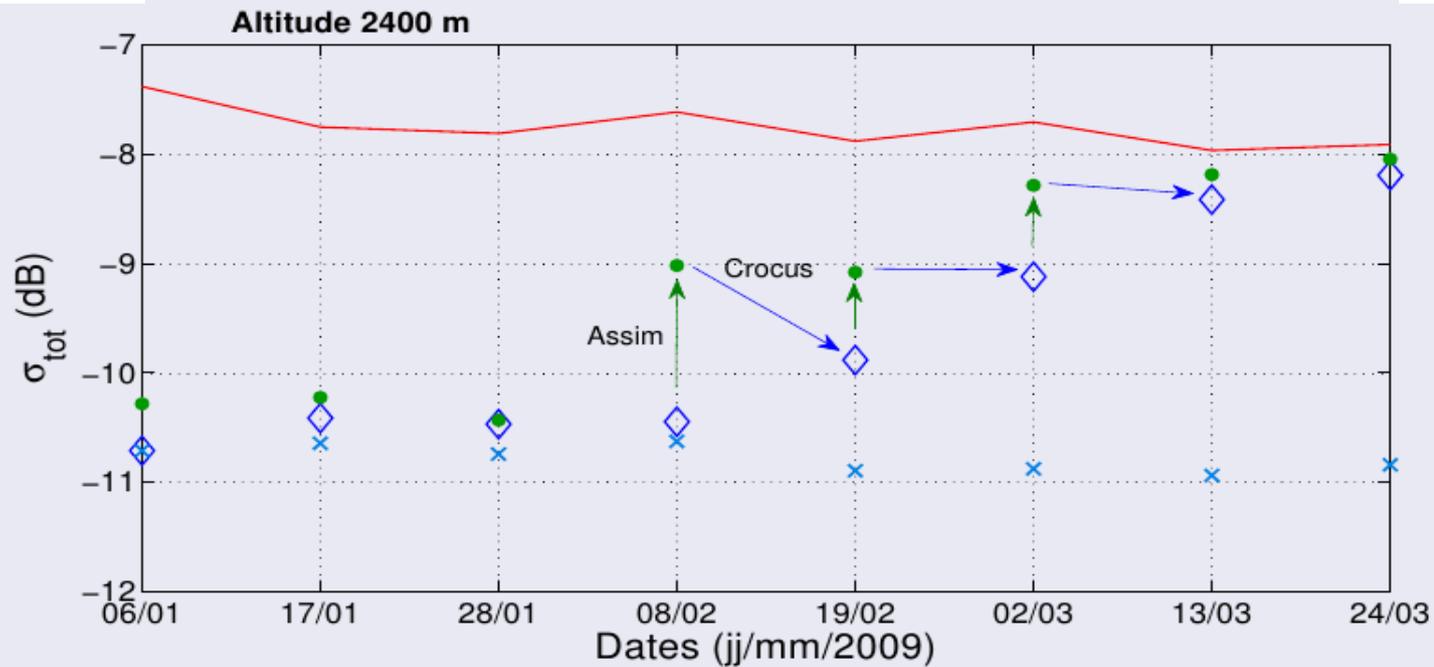


## Snowpack structure estimation:

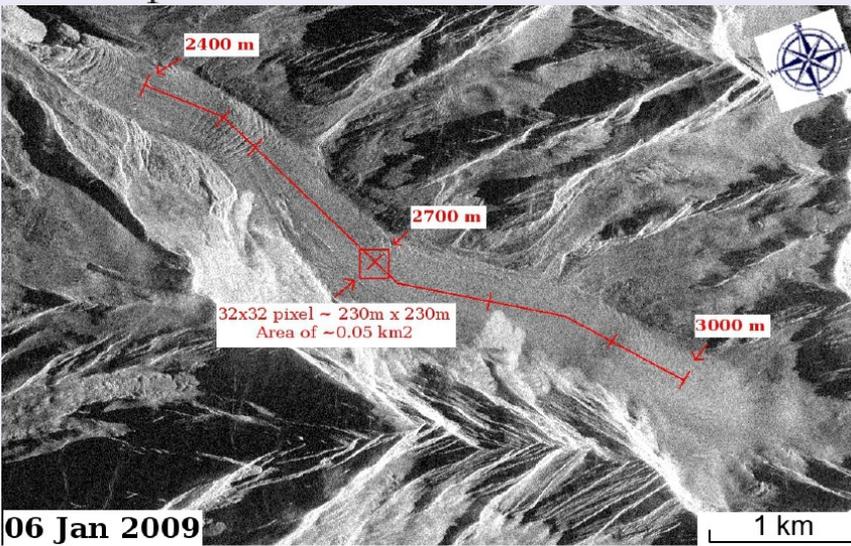
- resolution of an under-determined inverse problem (variational approach)
- solutions lie in the vicinity of SURFEX/Crocus predictions
- use of multi-temporal measurements: convergence of the estimation



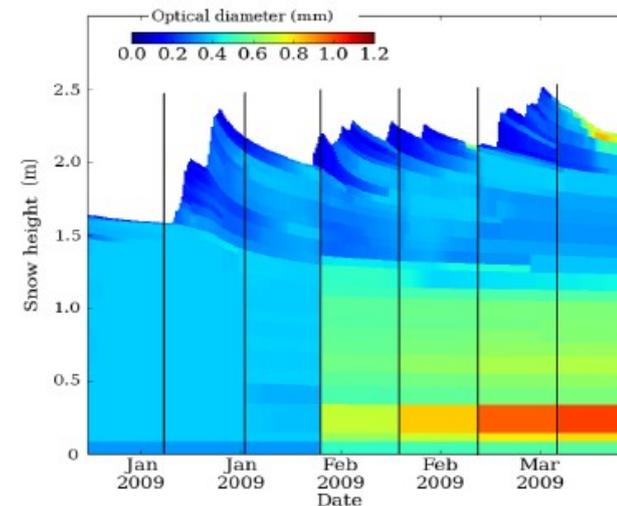
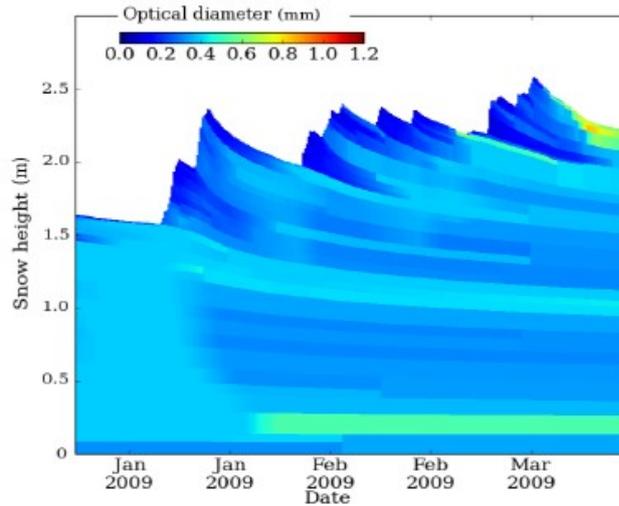
- $\sigma_{TSX}$
- ◇  $\sigma_{sim}$  - guessed profiles
- $\sigma_{sim}$  - assimilated profiles
- ×  $\sigma_{sim}$  - open-loop profiles



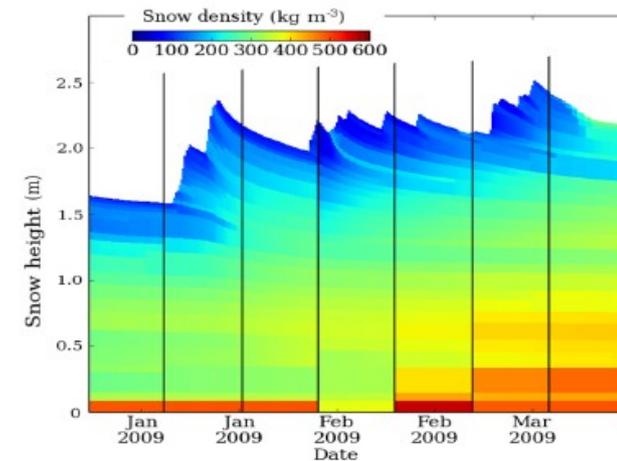
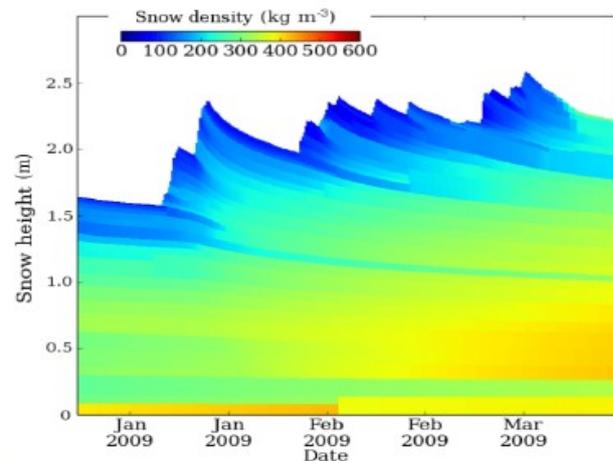
Temporal evolution of observed and simulated backscattering coefficients.



**Application to  
TSX time series  
over the  
Argentière glacier**



Temporal evolution of grain optical diameter, open loop (left) and assimilated (right).

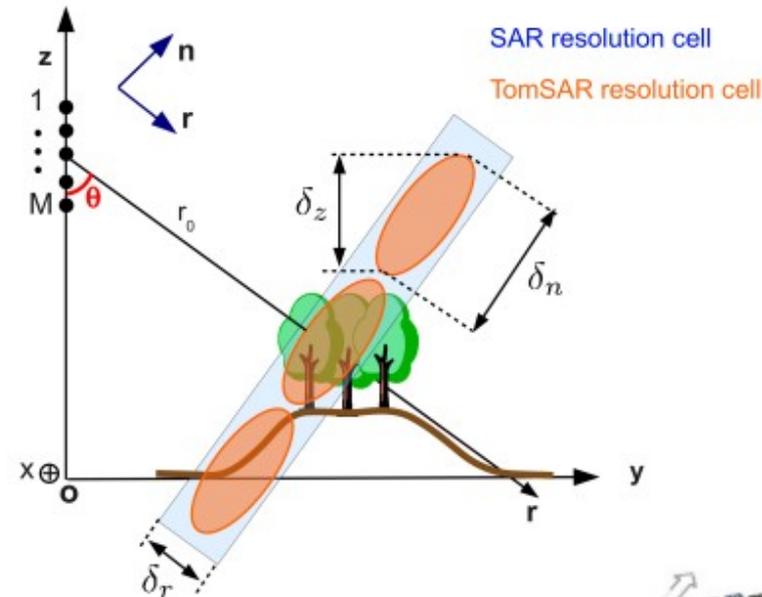
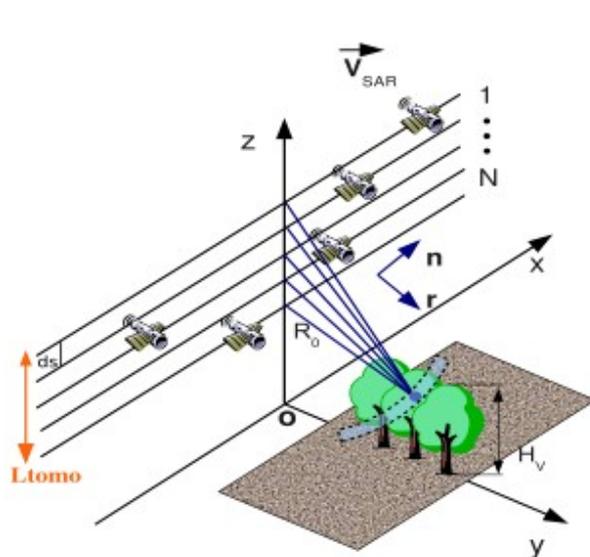


Temporal evolution of snow density, open loop (left) and assimilated (right).

## Multibaseline InSAR (MB-InSAR) tomography

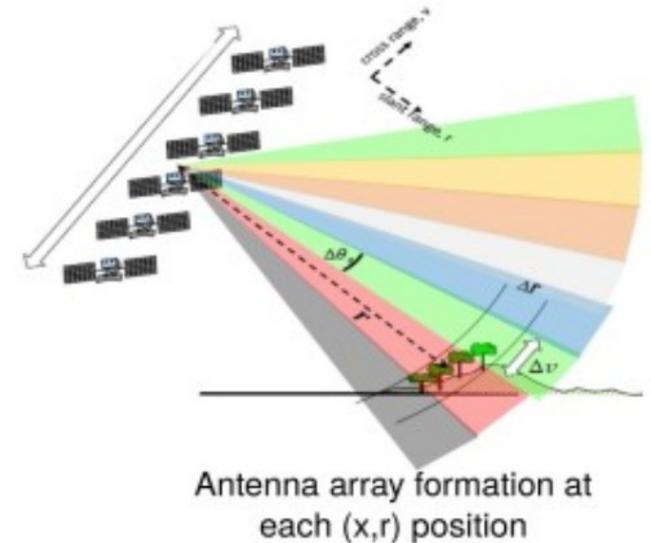
Several mixed scatterers → many across-track positions

### Acquisition geometry



### Vertical focusing

- Vertical aperture :  $L_{tomo}$
- Resolution :  $\delta_z = \delta_n \sin \theta$  with  $\delta_n = \frac{\lambda R_0}{2L_{tomo}}$

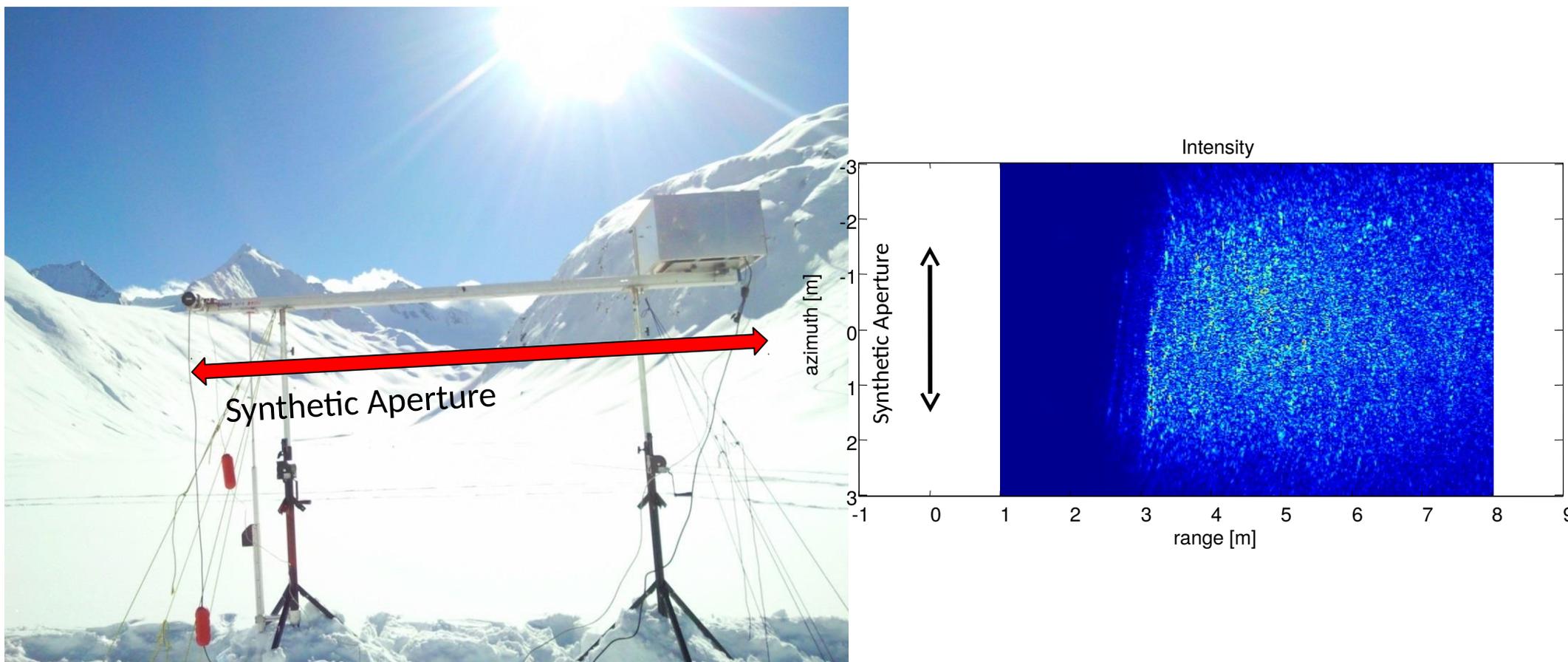


Measurements by a Ground based Synthetic Aperture Radar system, developed and implemented by the SAPHIR team at the University of Rennes 1

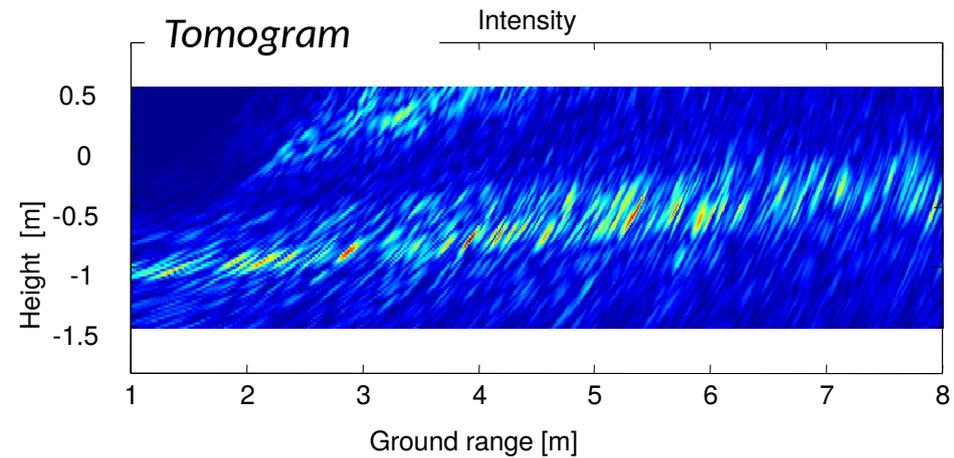
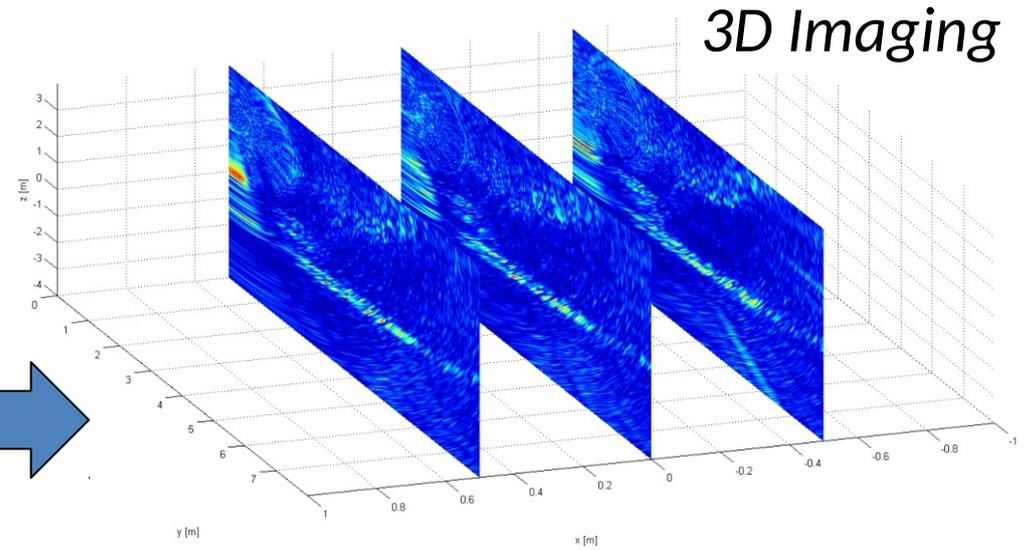
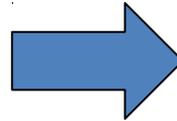
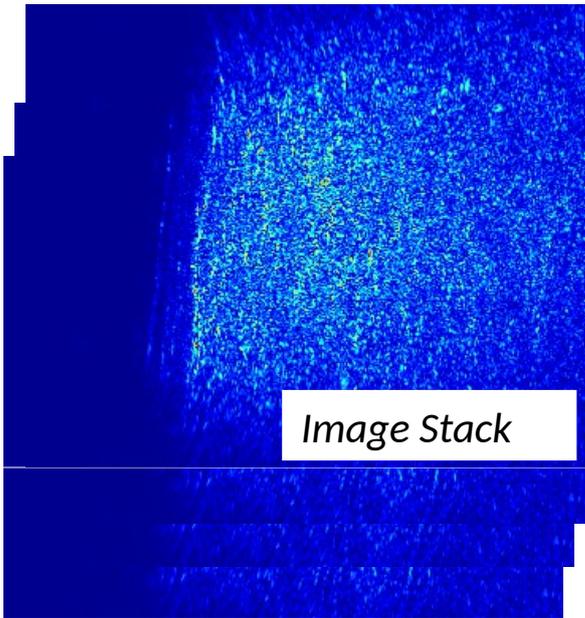
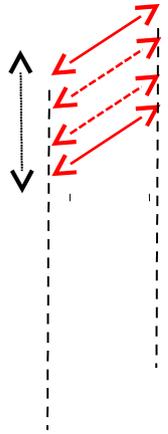
- 0 Signal Tx and Rx: VNA
- 0 Available frequency bands: 3 GHz to 20 GHz (C,X,Ku bands)
- 0 Dynamic range  $\approx 90$  dB
- 0 Sealed in a metallic box when operating 🔔 works under a snow fall
- 0 Box + VNA = 40 Kg



- Accurate sensor motion along a 3 m rail
- Fully automated
- Resolutions:  $Az < 5\text{cm}$ ,  $Rg = 3.75\text{ cm}$ ,  $El=10\text{ cm}$  centimeters at X- and Ku bands
- Max swath  $\approx 8\text{ m}$

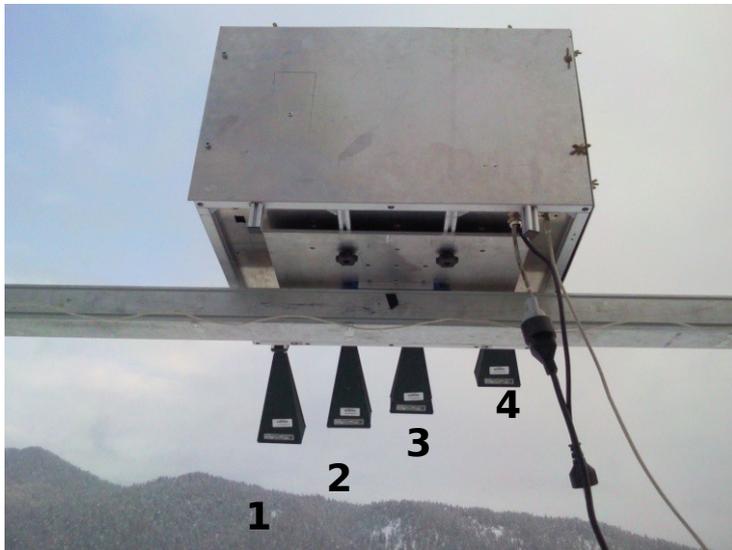


- 0 2D synthetic antenna: parallel vertical passes  
⇒ 3D resolution capabilities

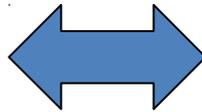


## IETR GBSAR: 3 Multi-Baseline acquisition modes

1. Combining different Tx and Rx antennas (multistatic Radar)



*Equivalent to 6 virtual passes*

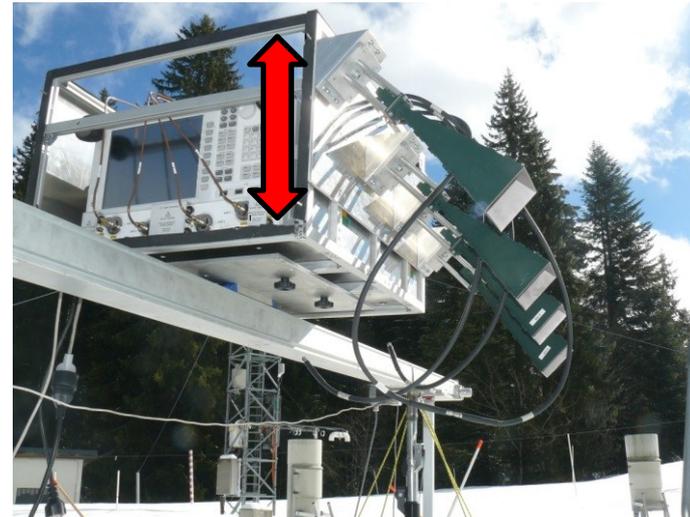


<u>Rx</u>	<u>Tx</u>
<u>1</u>	<u>2</u>
<u>1</u>	<u>3</u>
<u>1</u>	<u>4</u>
<u>2</u>	<u>3</u>
<u>2</u>	<u>4</u>
<u>3</u>	<u>4</u>



## IETR GBSAR: 3 Multi-Baseline acquisition modes

2. Varying the position w.r.t. the rail along the the VNA box



3. Varying rail height



○ Carried out in December 2010 over a Meteo-France snowfield at Col de Porte (French Alps)

○ Availability of in-situ data (Meteo-France/CEN)

- Snow grain diameter
- Liquid water content
- Density



○ Operated at X and Ku-Band

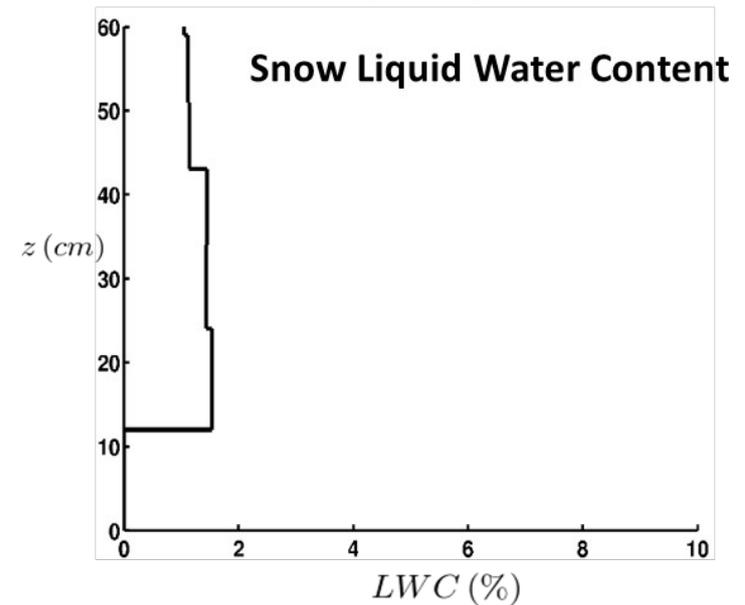
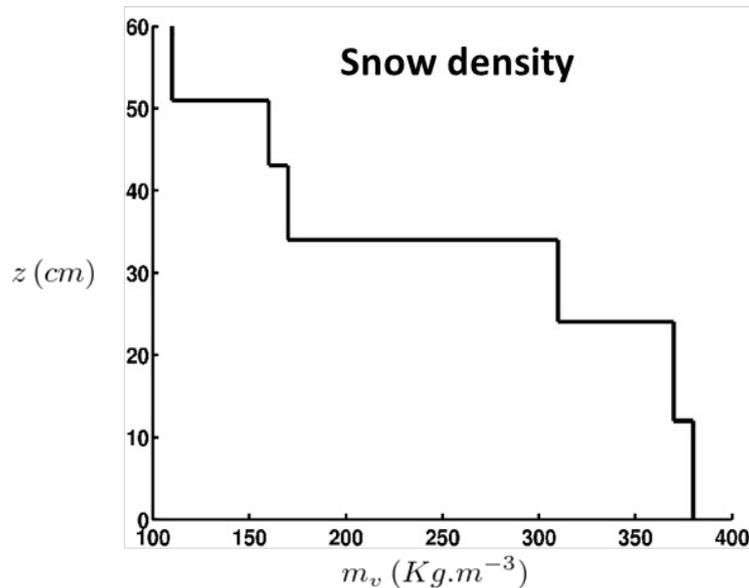
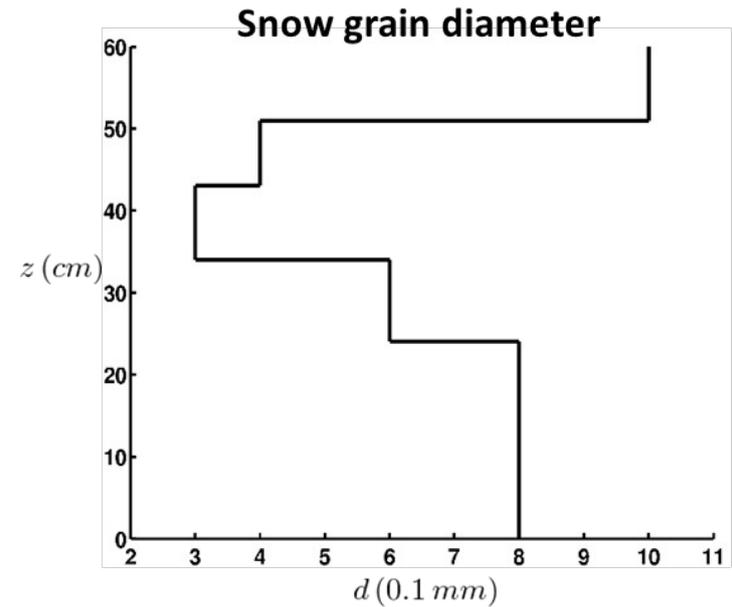
- Total transmitted bandwidth = 8 GHz
- Range resolution  $\approx 2$  cm
- Azimuth resolution  $\approx 2$  cm

○ 10 acquisitions: varying rail height

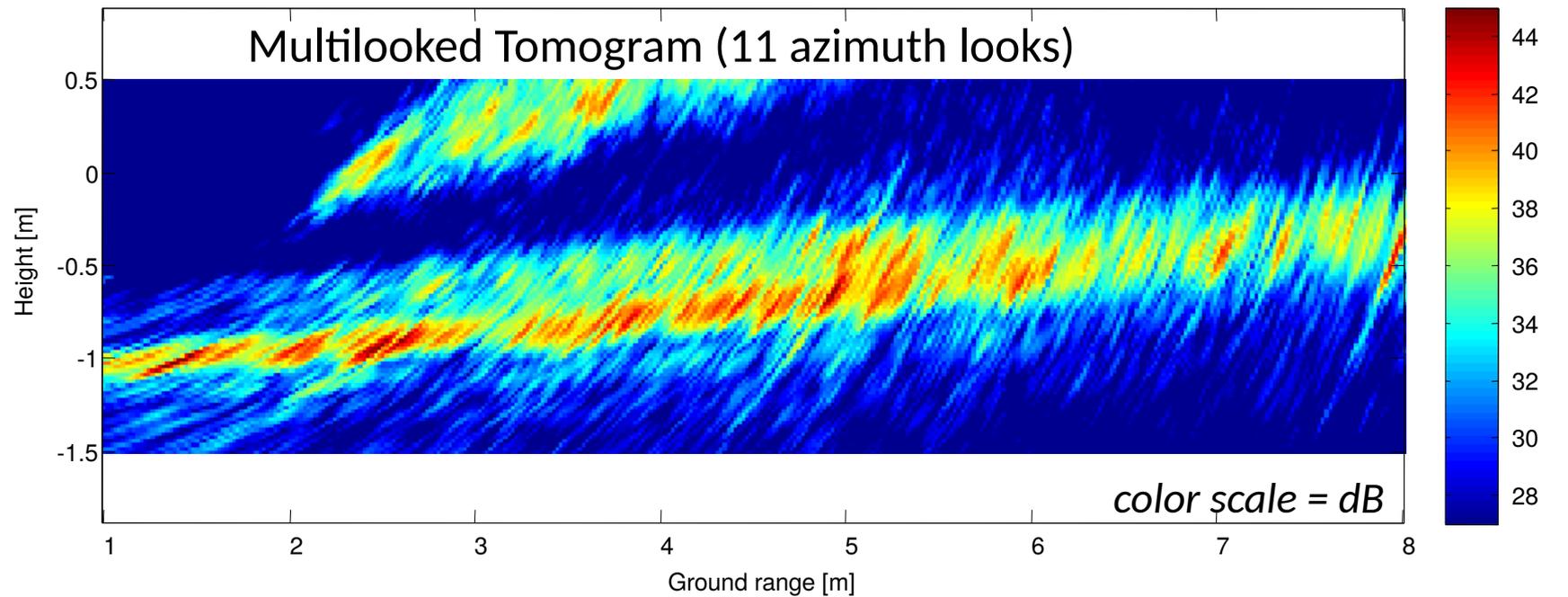
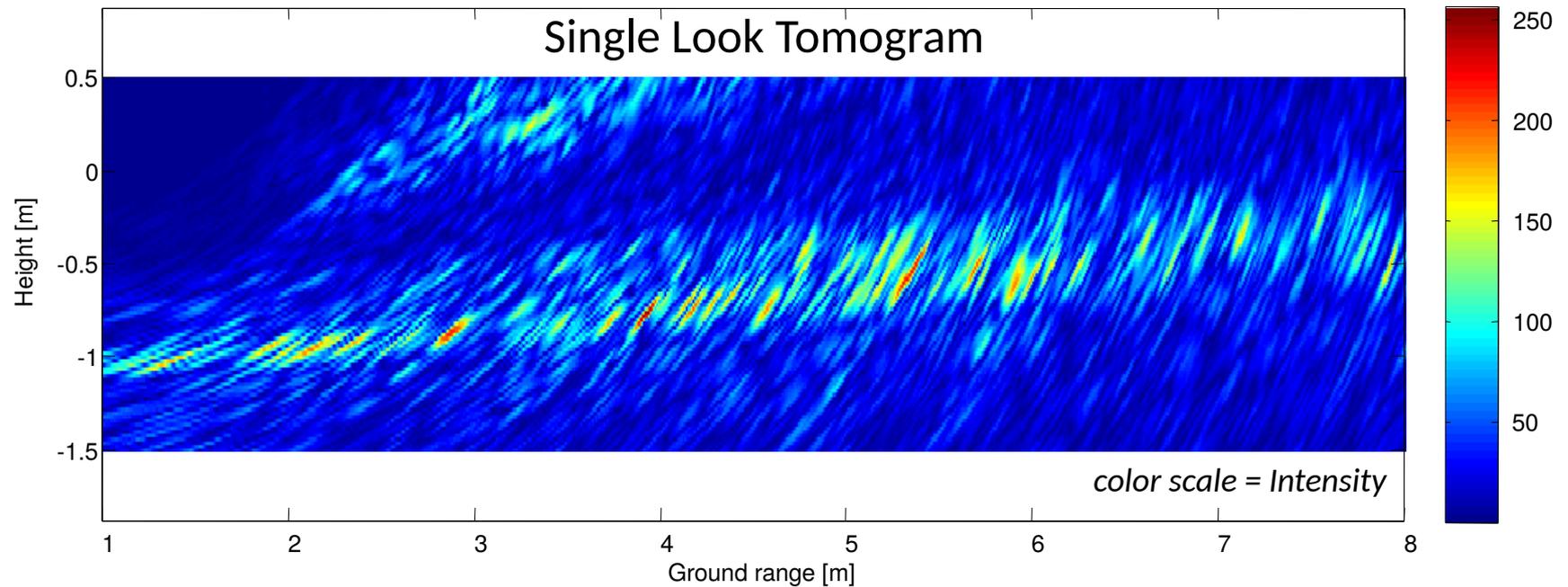
- Cross range resolution  $\approx 8$  cm
- Revisit time  $\approx 20$  minutes

# Campaign at Col de Porte – In-situ data

- Snow layer depth: approx. 60 cm
- Vertical snow profile probing (Meteo-France)
- Snow pack structure:
  - Upper layer: low density of fresh snow
  - Middle layer : intermediate density, smaller grains
  - Lower layer: high density and size, very compact snow/ice

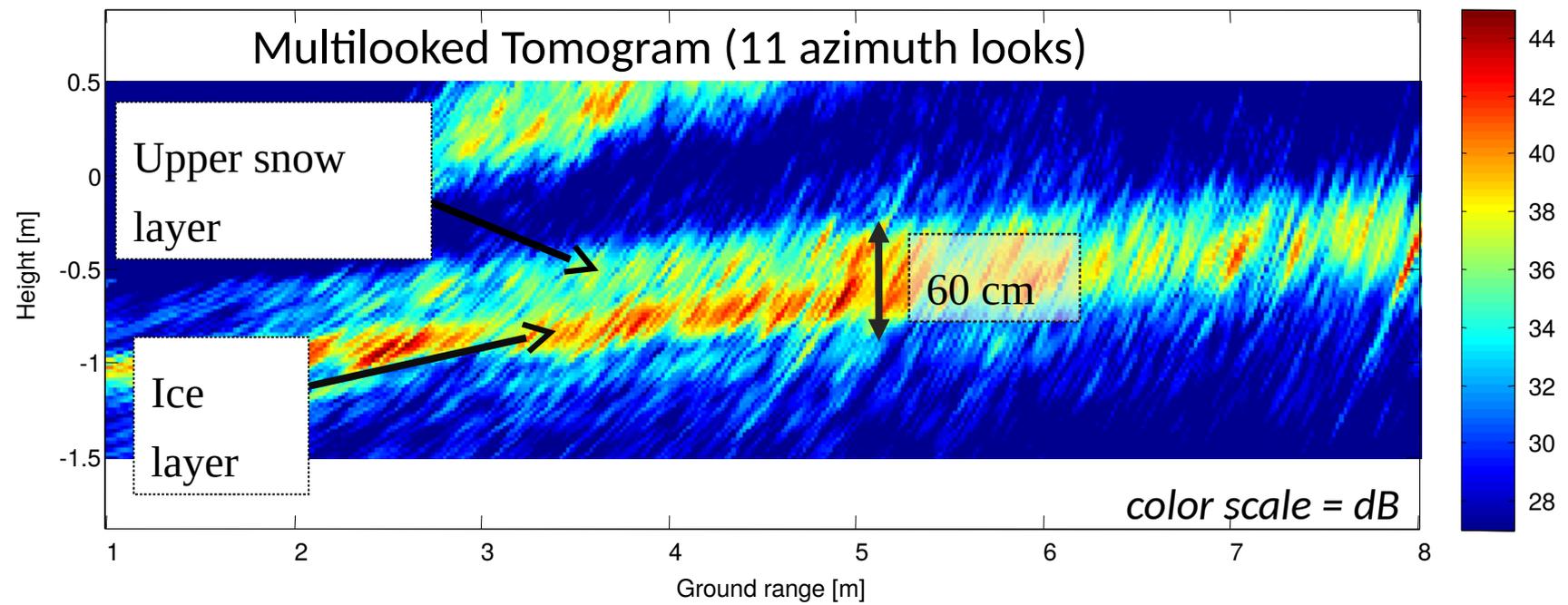


# Wide band imaging (8.2 GHz - 16.2 GHz)



## Physical Interpretation

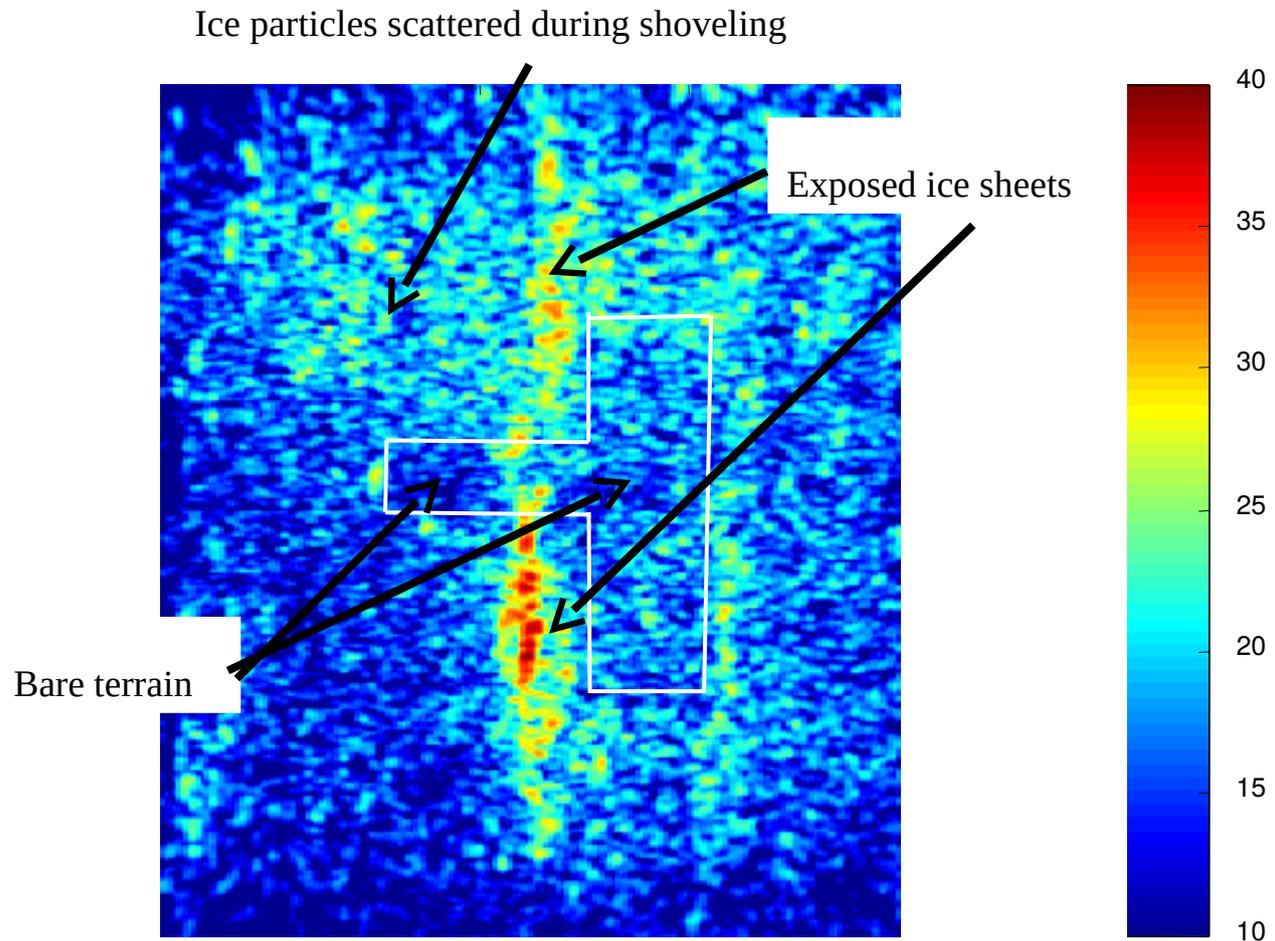
- Observed thickness  $\approx 60$  cm; Observed slope  $\approx 7$  cm/m (rising)
- Strongest contribution from the bottom layer (buried ice/very dense snow)
- Upper snow layer: intermediate intensity



Digging of a T-shaped hole: terrain backscattering contribution

During digging the burried was deployed aside on the snow layer

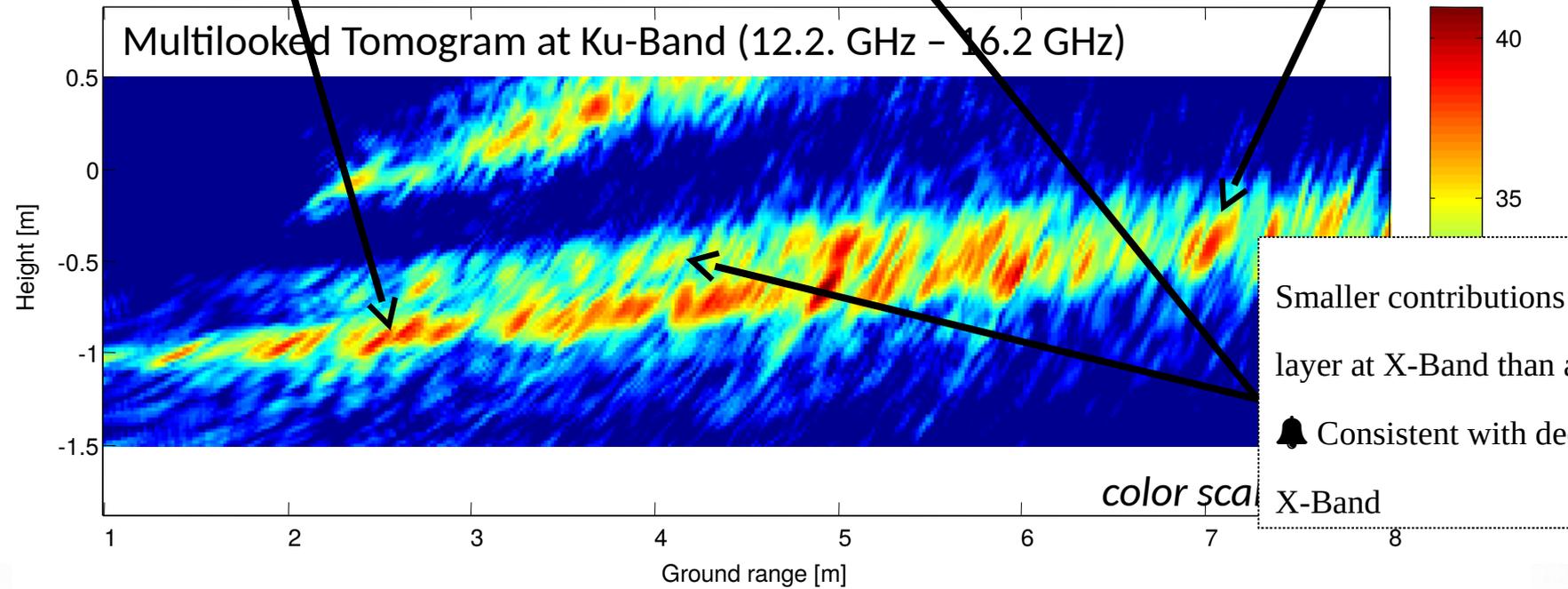
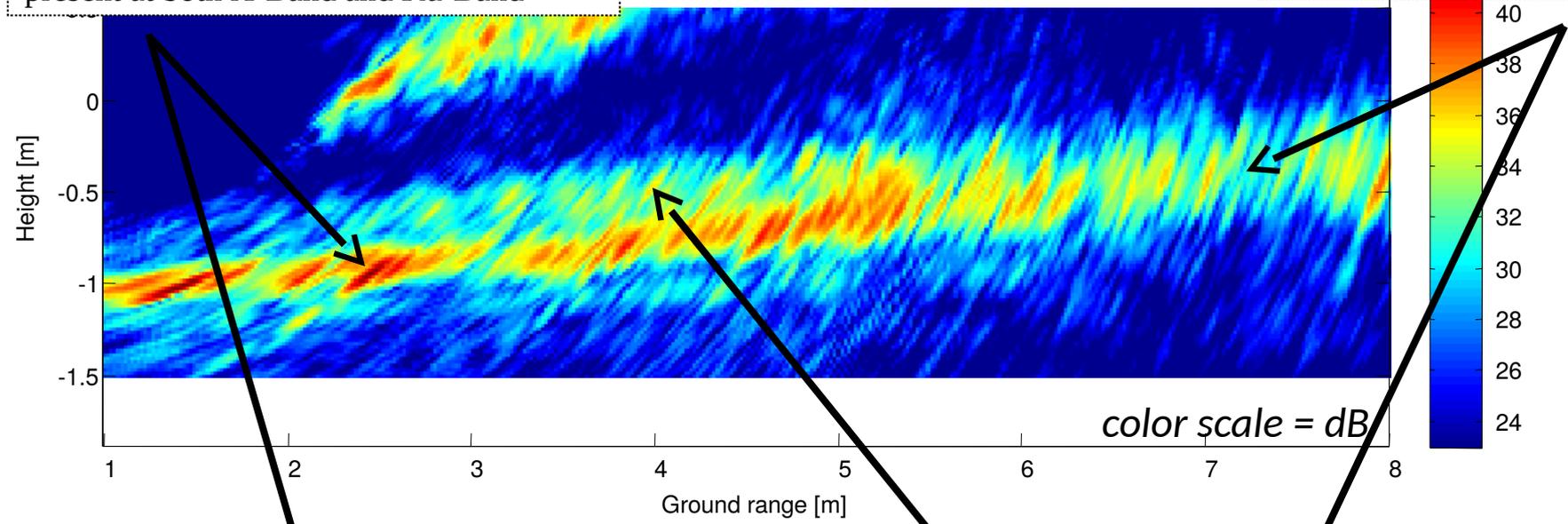
contributions from exposed ice sheets  
**dominate those from the terrain by  
over 30 dB**



# Imaging at X - and Ku-Band

Contributions from the ice-layer are present at both X-Band and Ku-Band

Grazing angles show higher returns at Ku-Band than at X-Band  
↔ Rough interface effects ?



Smaller contributions from the upper snow layer at X-Band than at Ku-Band  
🔔 Consistent with deeper penetration at X-Band

- AlpSAR ESA campaign, led by ENVEO, Austrian Alps, Feb. 2013
  - Snowpit data, GPR, Airborne SAR, **GBSAR**

- Two sites:

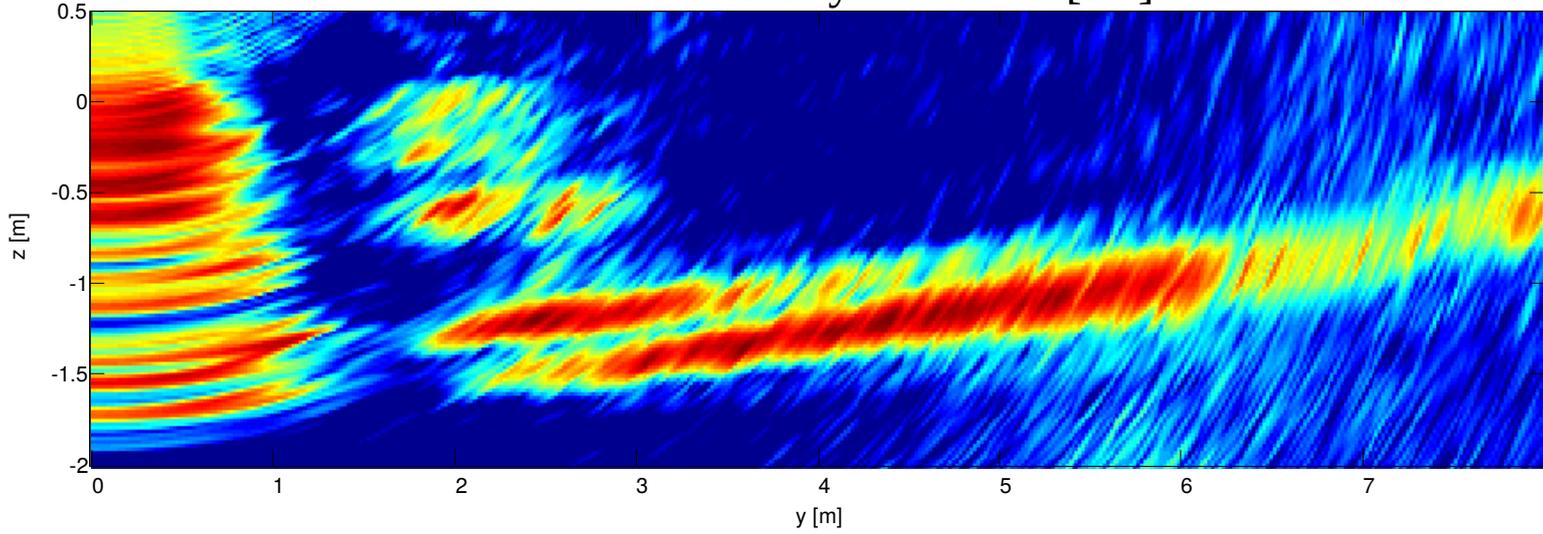


- GB-SAR operated at X and Ku-Band
  - Total transmitted bandwidth = 4 + 4 GHz
  - Range resolution  $\approx 4$  cm
  - Azimuth resolution  $\approx 2$  cm

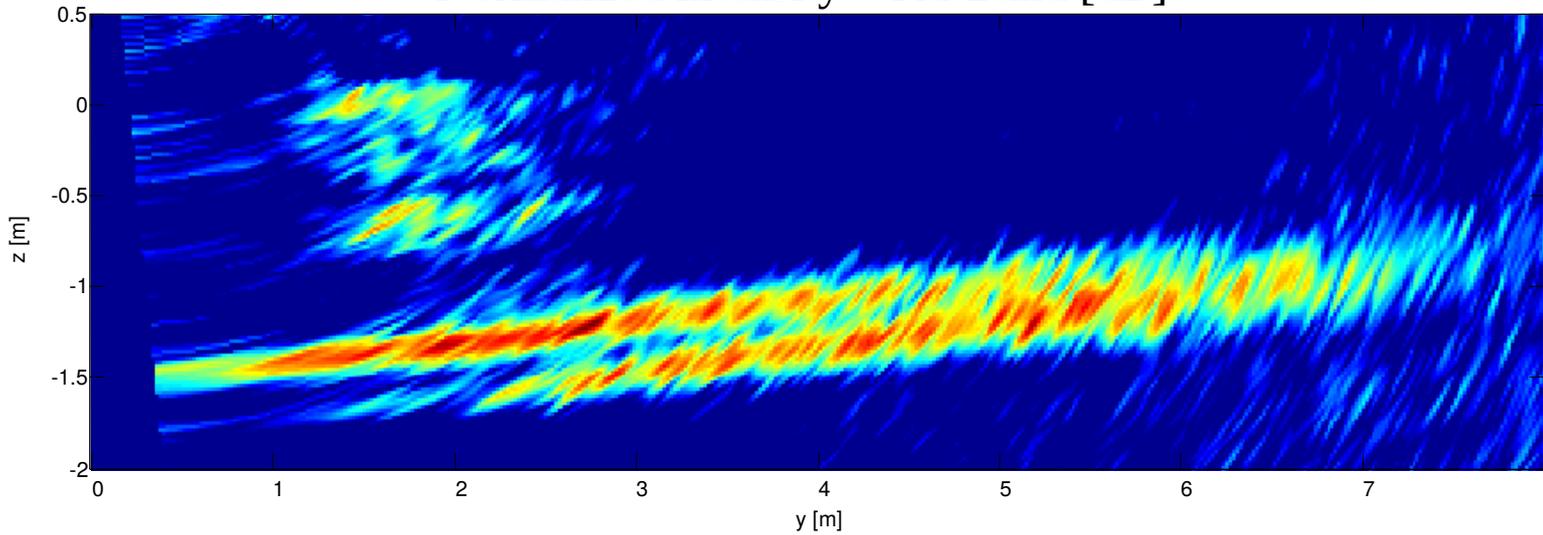
- Multiple multistatic passes
  - Vertical resolution  $\approx 10$  cm (Ku-band), 15 cm (X-Band)

- Remarks
- Neat imaging
  - 5 surfaces
  - Strongest returns are associated with the two bottom layers

### Normalized intensity – X-Band [dB]



### Normalized intensity – Ku-Band [dB]



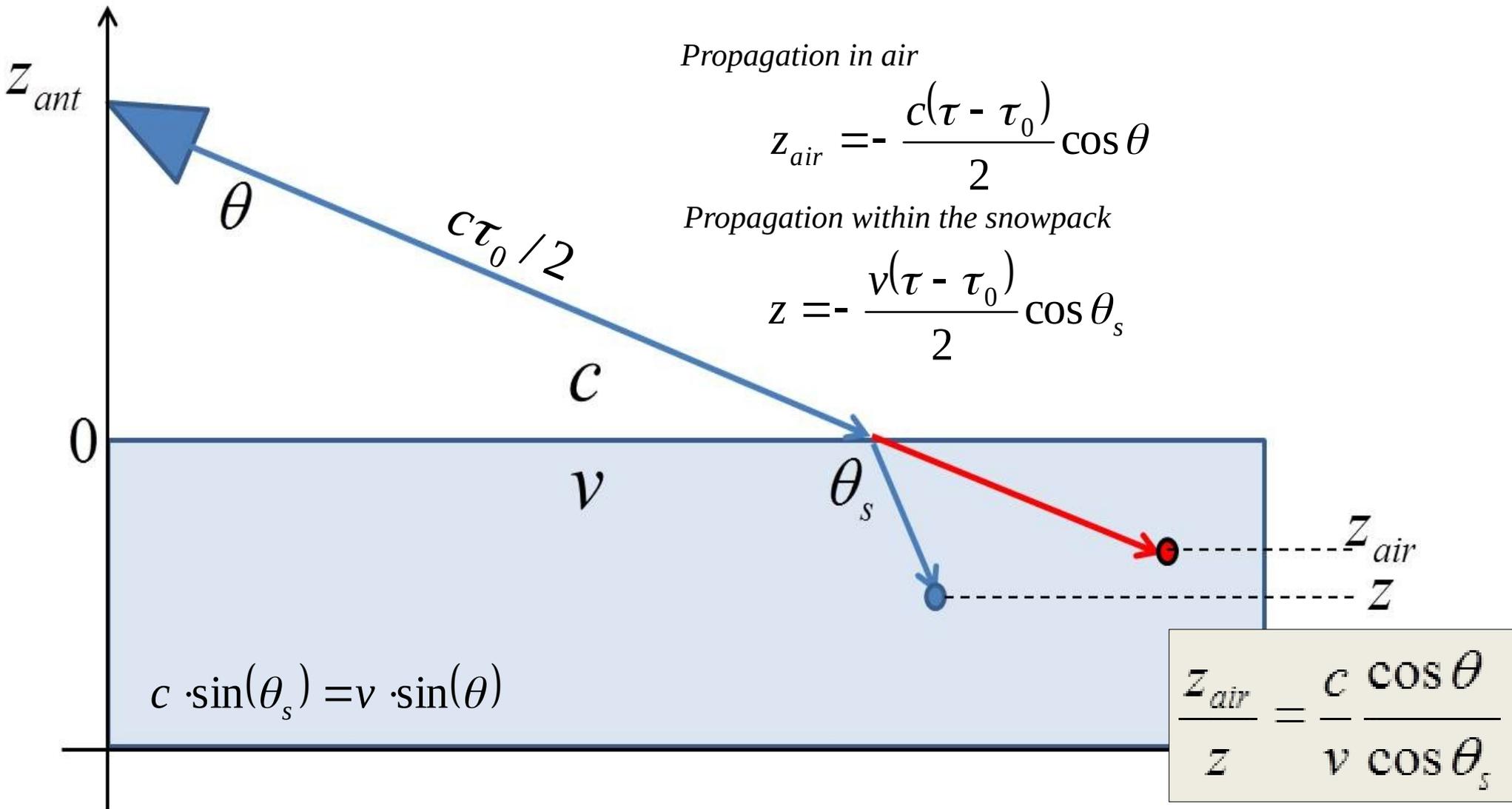
**Snowpit data:**  
snowpack thickness = 140 cm

Normalized intensity is presented to highlight contrasts

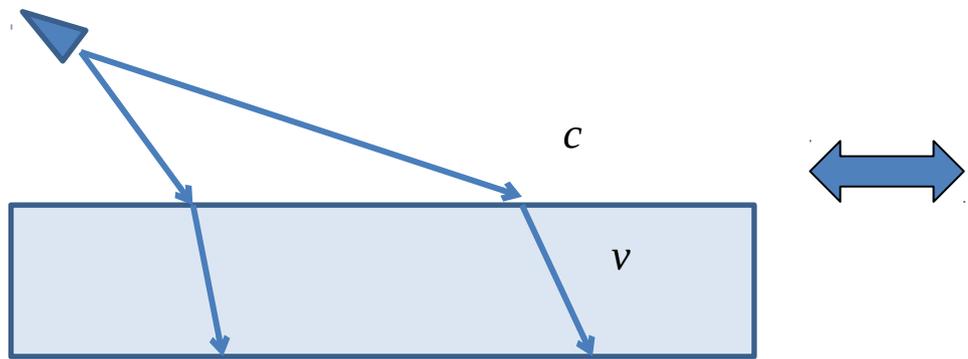
# Effect of propagation velocity

Localization in the (y,z) plane:

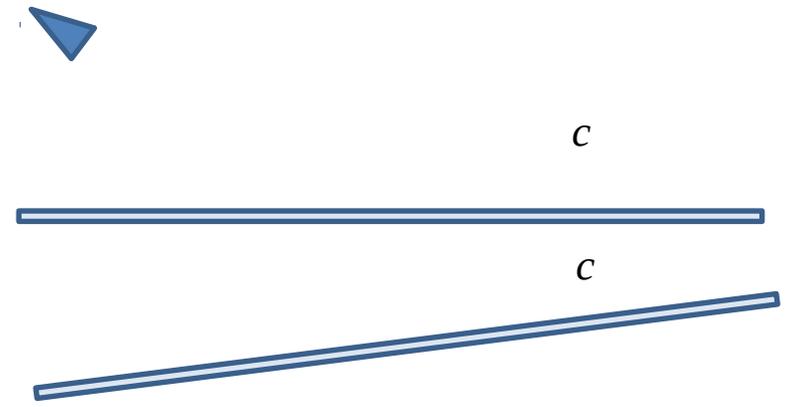
- i) delay ( $\tau$ ), converted into a distance based on the knowledge of propagation velocity
- ii) wave direction on the receiving array, that provides the incidence angle



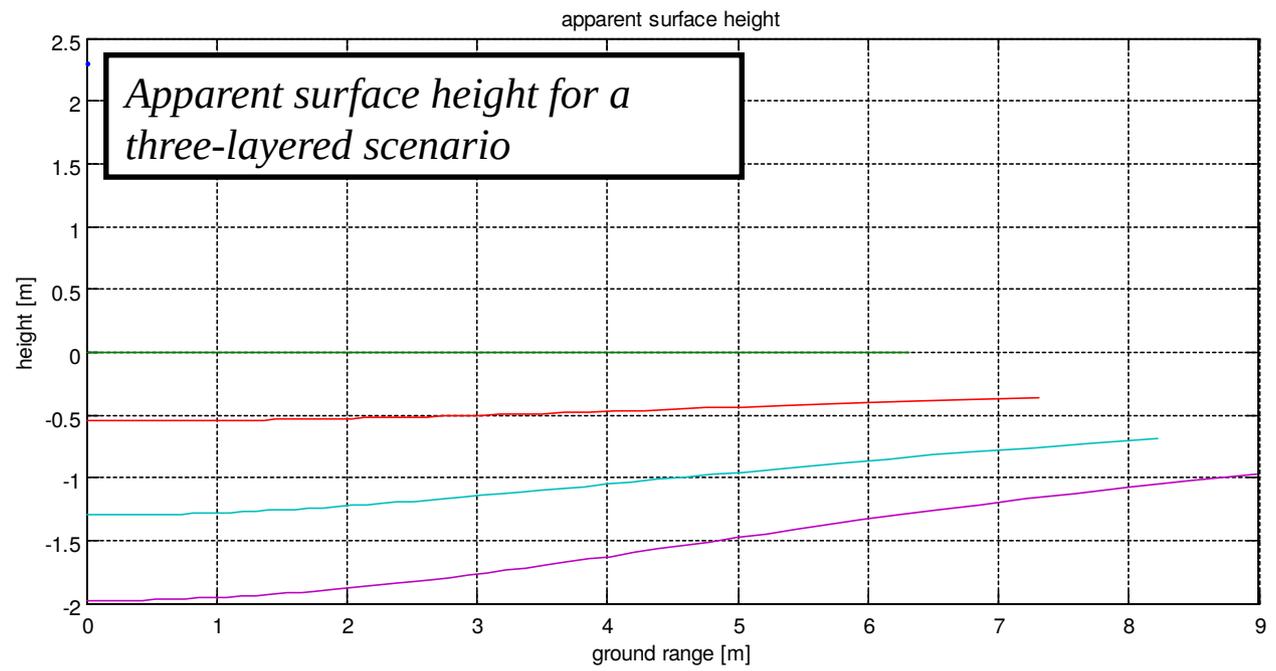
Real scenario



Resulting vertical section

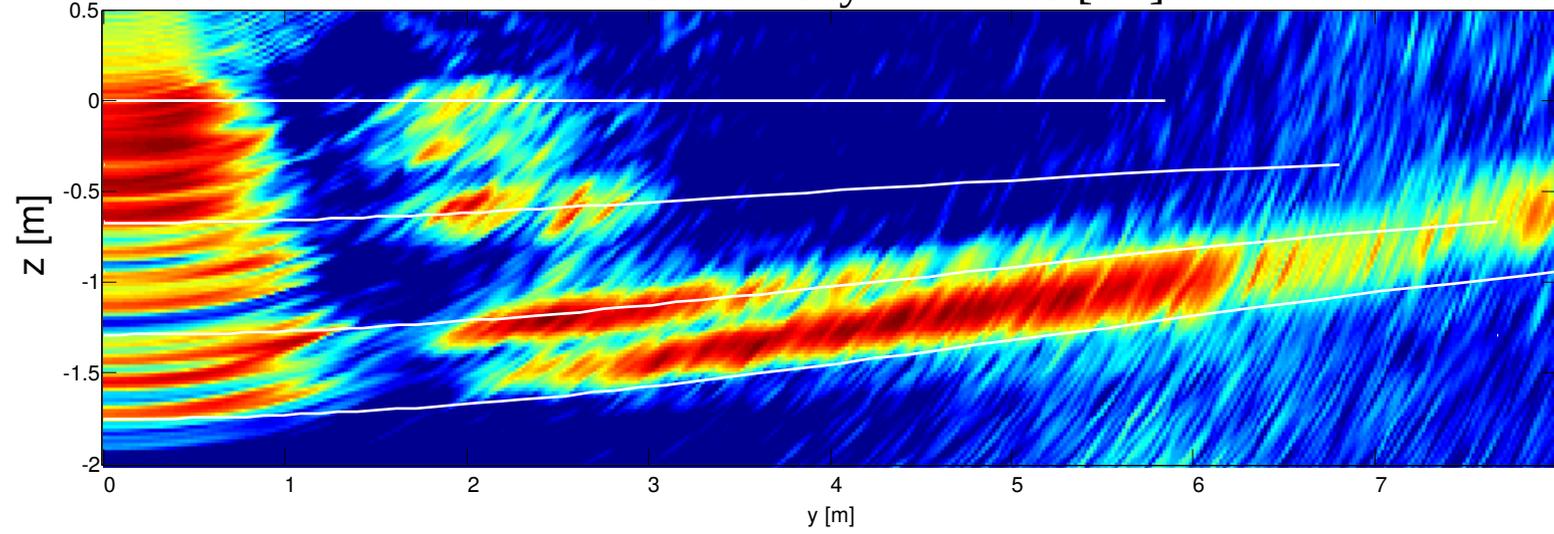


$$\frac{z_{air}}{z} = \frac{c \cos \theta}{v \cos \theta_s}$$



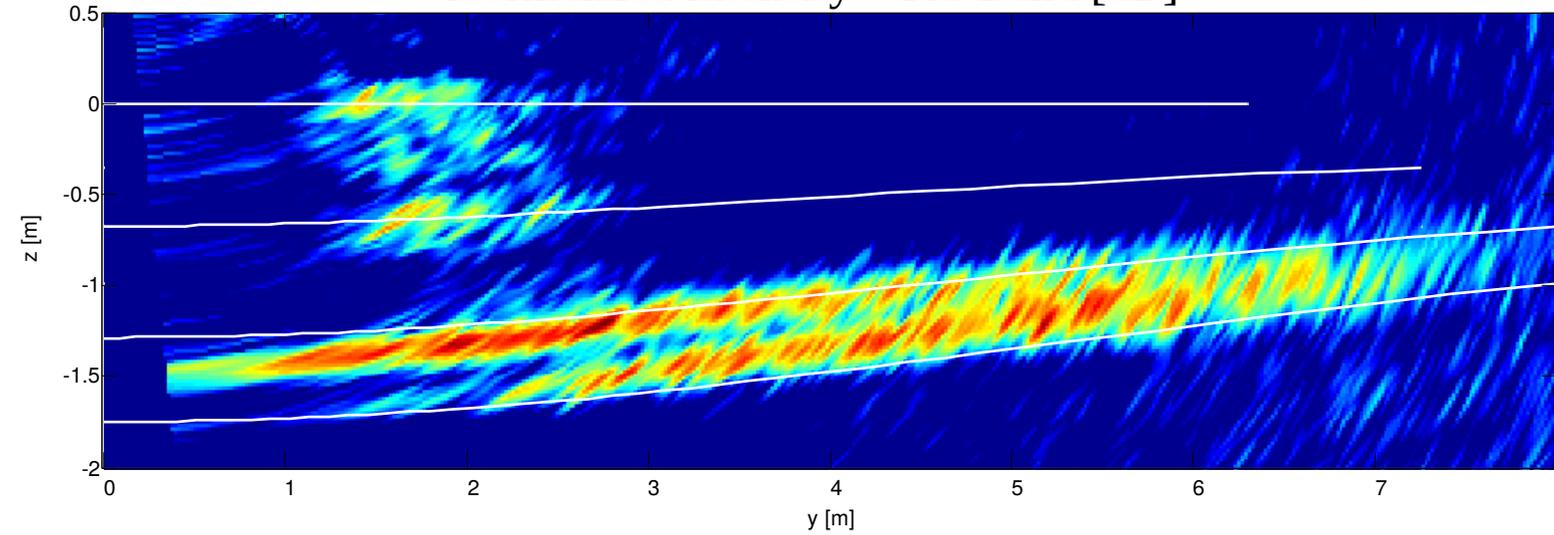
- Remarks
- Neat imaging
  - 5 surfaces
  - Strongest returns are associated with the two bottom layers

### Normalized intensity – X-Band [dB]



Apparent surface heights for  $v = c/1.25$

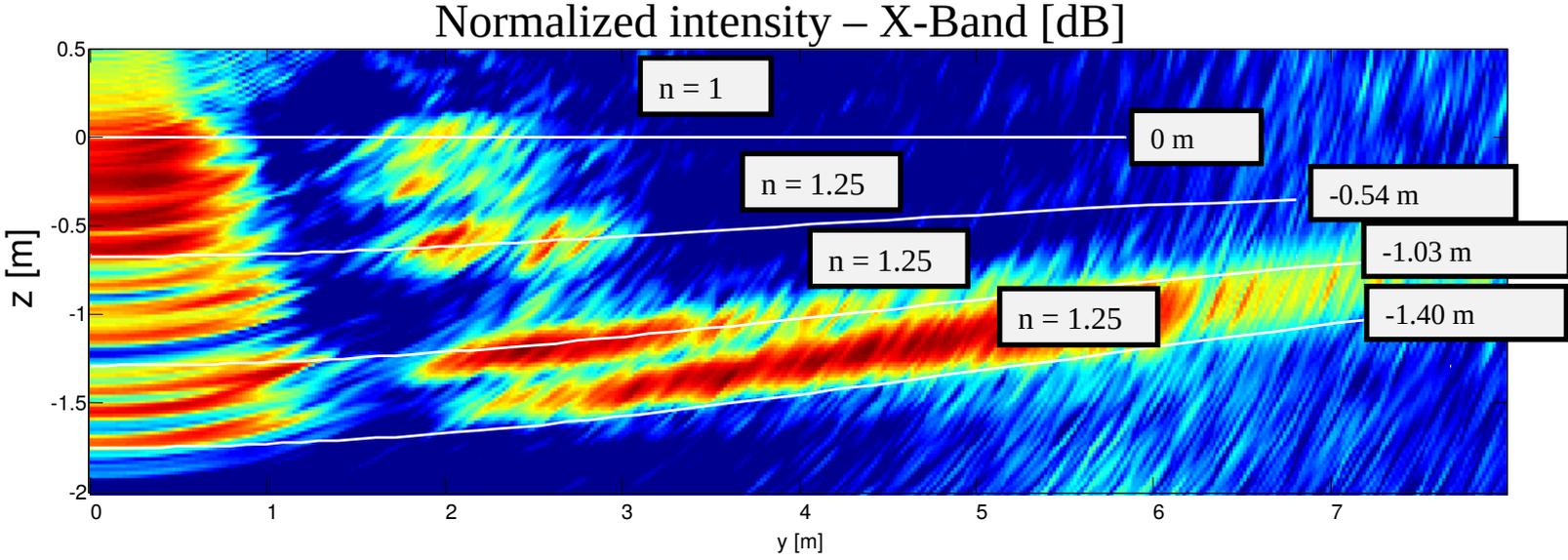
### Normalized intensity – Ku-Band [dB]



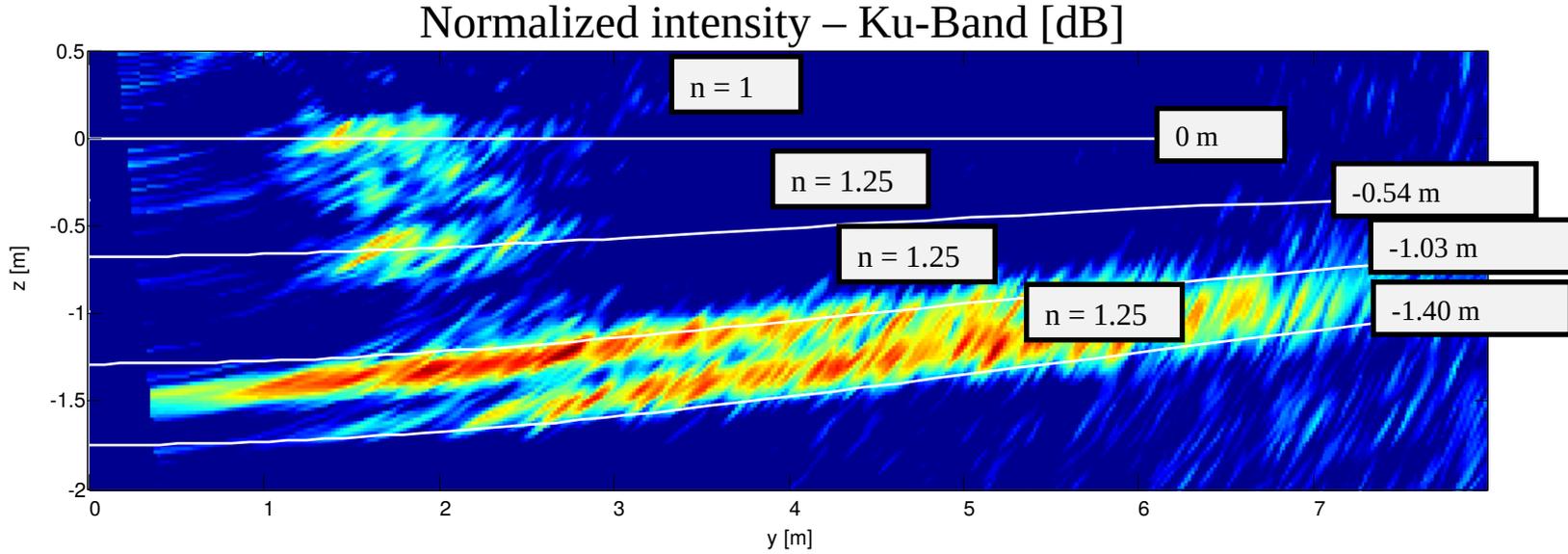
**Snowpit data:**  
snowpack thickness = 140 cm

Normalized intensity is presented to highlight contrasts

- Remarks
- Neat imaging
  - 5 surfaces
  - Strongest returns are associated with the two bottom layers



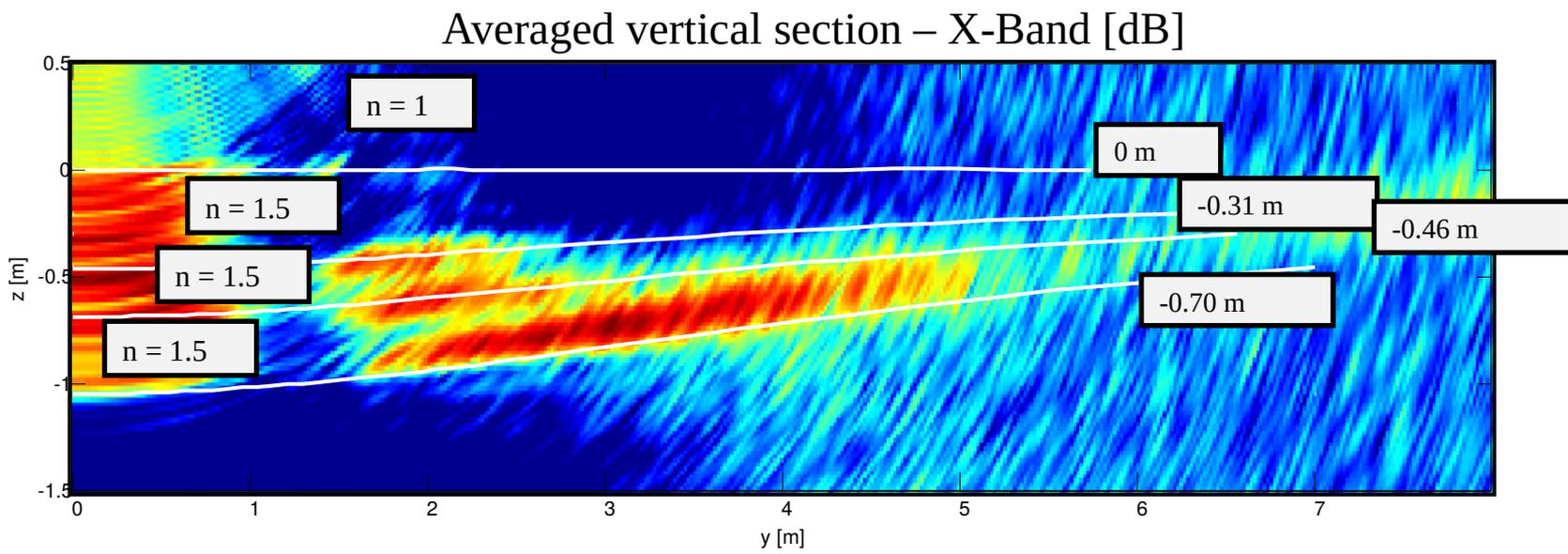
Apparent surface heights for  $v = c/1.25$



**Snowpit data:**  
snowpack thickness = 140 cm

Normalized intensity is presented to highlight contrasts

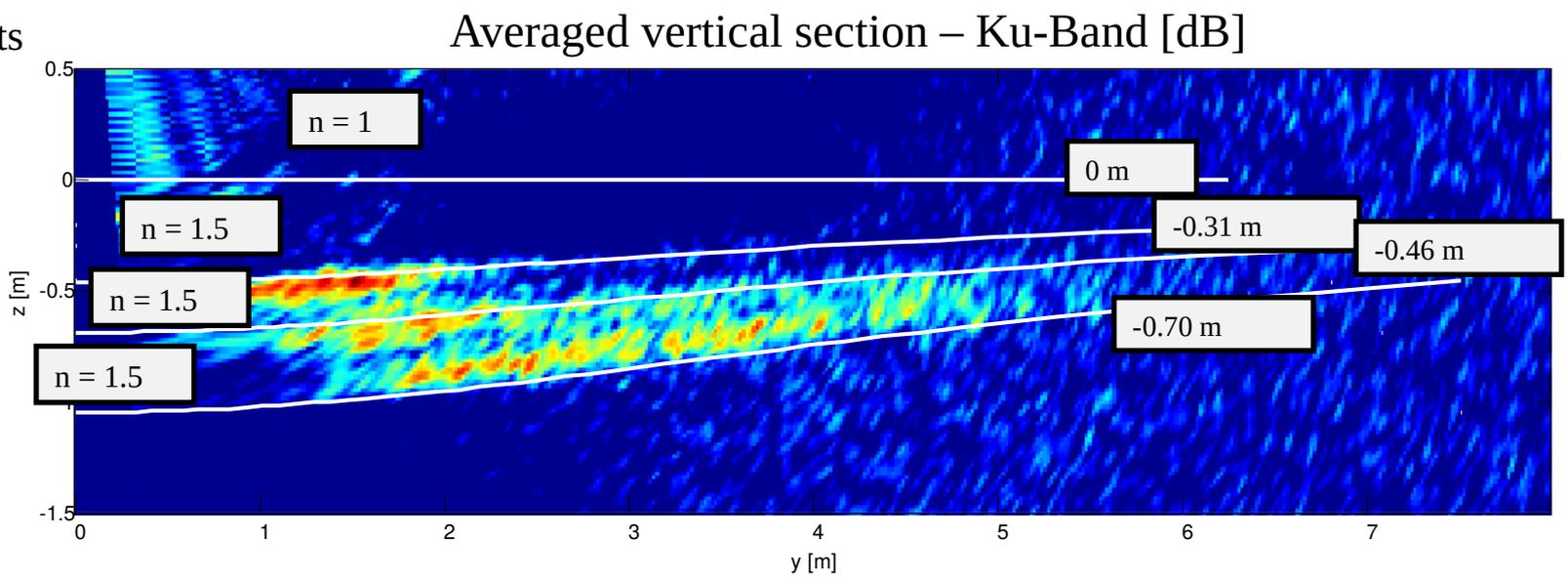
- Remarks
- Neat imaging
  - 4 surfaces
  - Weak returns from the snow/air interface
  - Strongest returns are associated with the bottom layers (X-Band) or middle (Ku-Band) layer



Apparent surface heights for  $v = c/1.5$

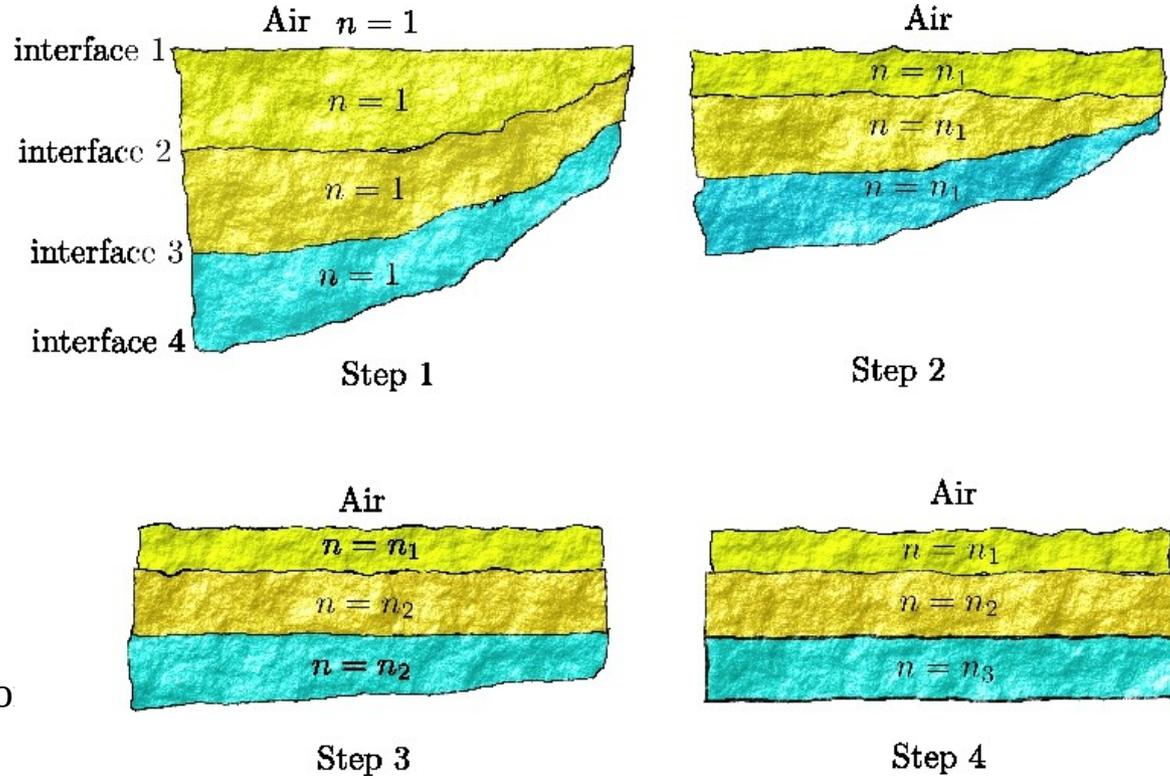
**Snowpit data:**  
snowpack thickness = 70 cm

Normalized intensity is presented to highlight contrasts



Iterative procedure for estimation of refractive indices:

- Assumption : horizontal snow layers with horizontal snow slabs;
- Main idea : choose refractive indices for the identified layers to make the appearance of the detected interfaces horizontal on the final tomogram;
- Iterative procedure :



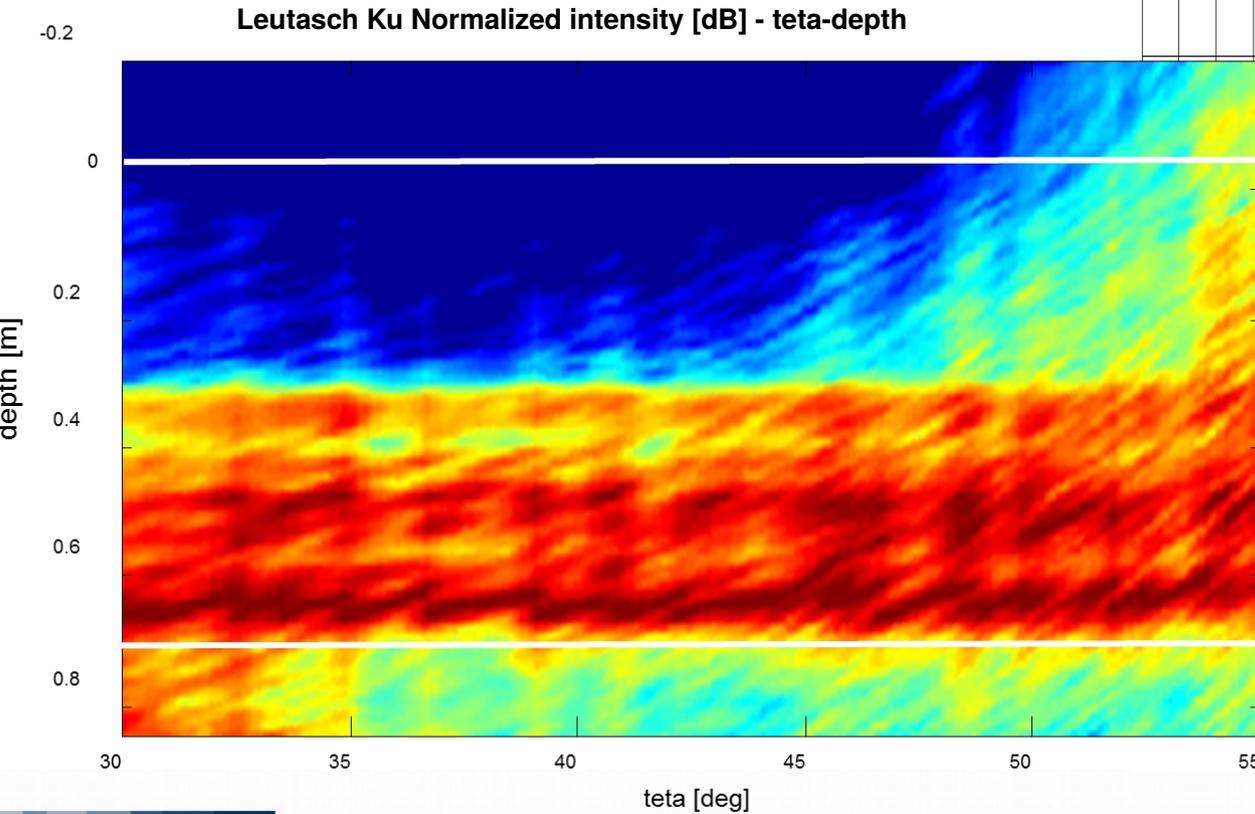
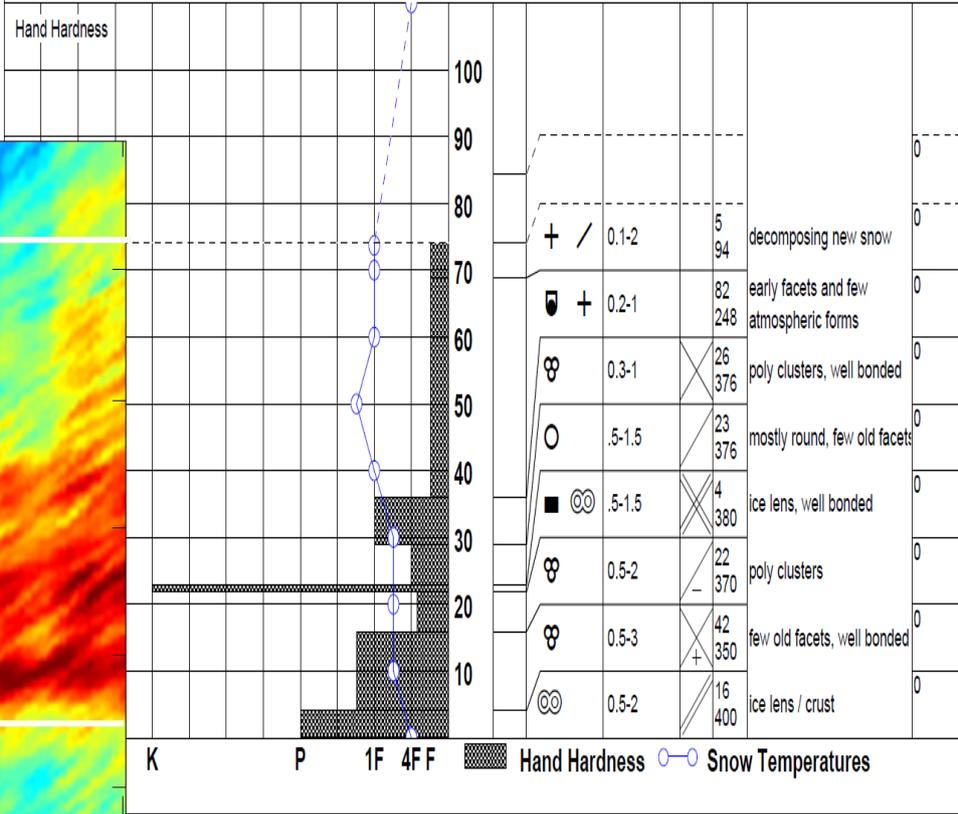
○ Distance computatio

$$\|\vec{\nabla}d(\vec{r}, \vec{r}_a)\|^2 = n^2(\vec{r})$$

# Connection to in-situ data: Leutasch

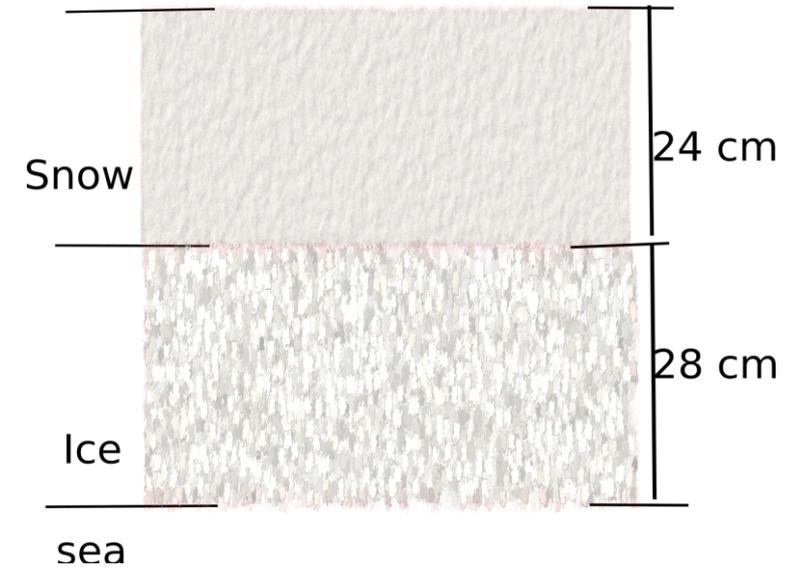
- Dominant scattering from bottom layers
- Results are largely independent on the incidence angle
- ☺ Retrieved vertical structure consistent with snowpack hand-hardness from snow-pit measurement

<b>SNOW COVER PROFILE</b>		Obs Elder	Profile Type	Other Profile
ALPSAR 2012/13		Obs2 Bowker	No	1
Leutasch GbSAR 1		DR	Surface Roughness	Smooth
Date	20/02/2013	Time	14:17	Penetration Foot Ski
Location Leutasch		Air Temp	0.0 C	Surface Temp -2.0 C
H.A.S.L.		Wind Loading	Sky Cond ☉ Broken Clouds with thin cloud/overcast	
Aspect	N/A	0°	Incline	0°
HS	74	HSW	219	ρ 297 R
Lat	N46.22.49	Long	E011.09.48	Wind Moderate 26-40 km/hr North East
Notable		Photo		





Data acquisition carried out in March 2013 at the Kattfjord, Tromsø, Norway

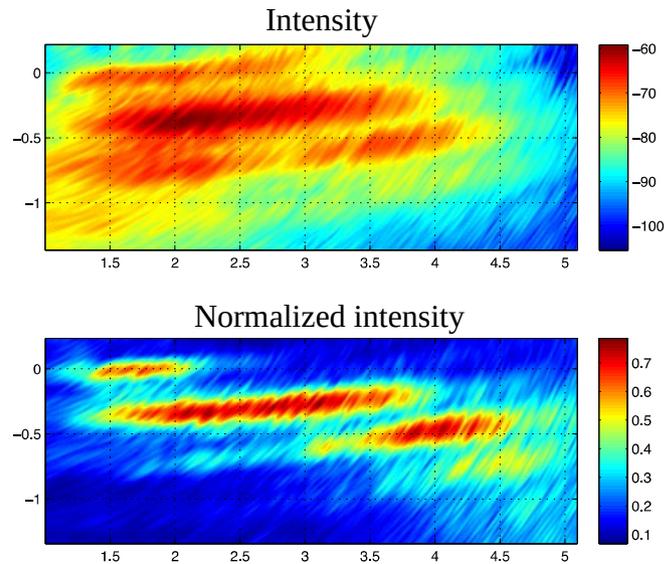


- Seasonal ice – life of 3-4 months
- Tomographic X-band measurements at VV and HV
- Temperature from  $-8^{\circ}$  to  $-2^{\circ}$
- The fjord ice can be representative of low salinity sea ice (fresh water from surrounding mountains)
- Dry snow cover on top
- Significant amount air bubbles within the ice layer
  - 0.5 mm to 7 mm diameter
  - Irregularly shaped
  - Randomly oriented

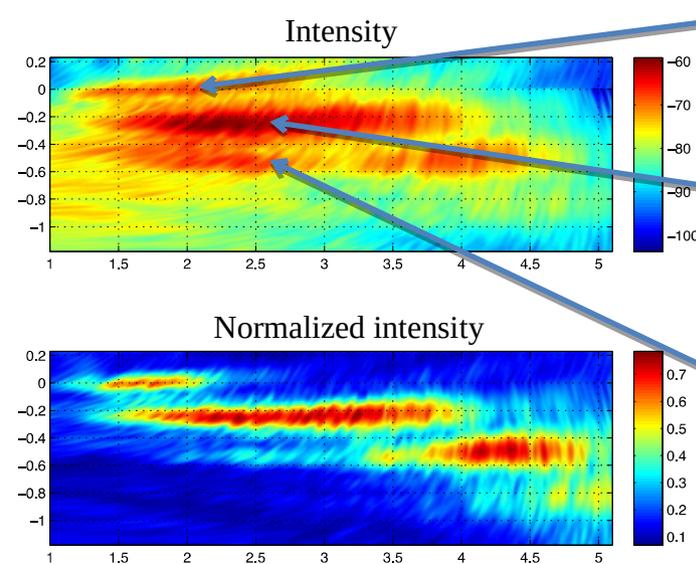


- Same tilt effect as snow-pack tomography
- Corrected assuming
  - refractive index of snow = 1.4
  - refractive index of fjord ice = 1.7
- Normalized intensity is presented to highlight contrasts (interfaces)

## Uncorrected



## Corrected



**Air-snow**

**Snow-ice**

**Ice-seawater**

Snow

Ice

seawater

0

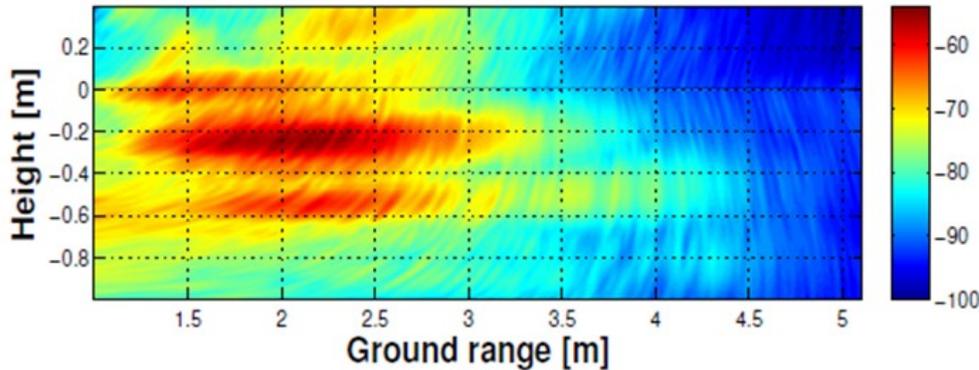
- 24 cm

- 52 cm

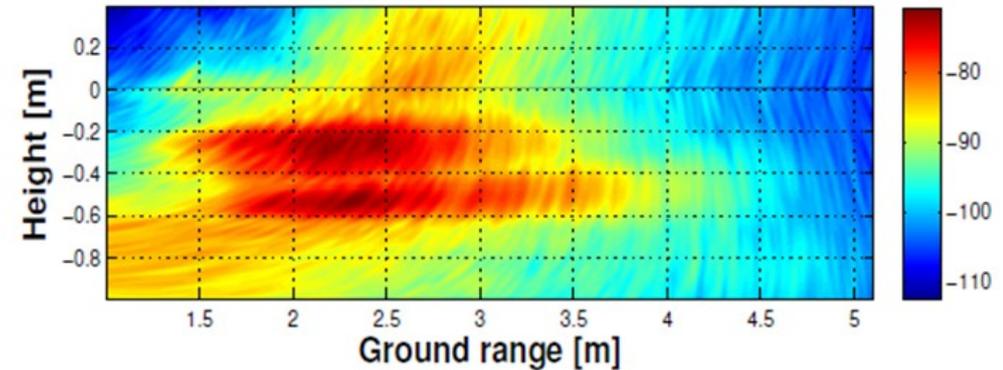
- Three clearly visible interfaces
  - Air/snow
  - Snow/ice
  - Ice/seawater

## 0 VV & HV tomography

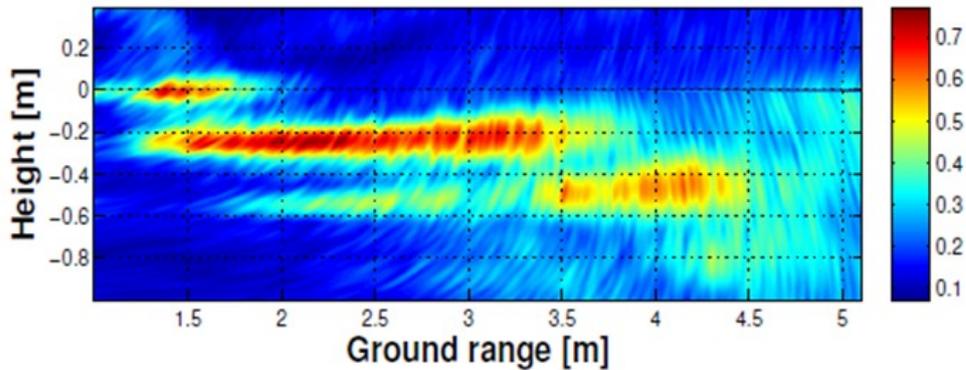
Corrected intensity (VV)



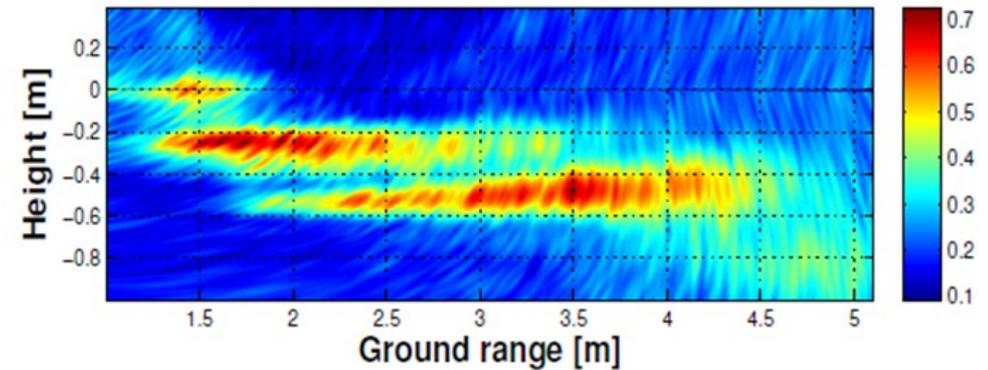
Corrected intensity (HV)



Corrected normalized intensity (VV)



Corrected normalized intensity (HV)



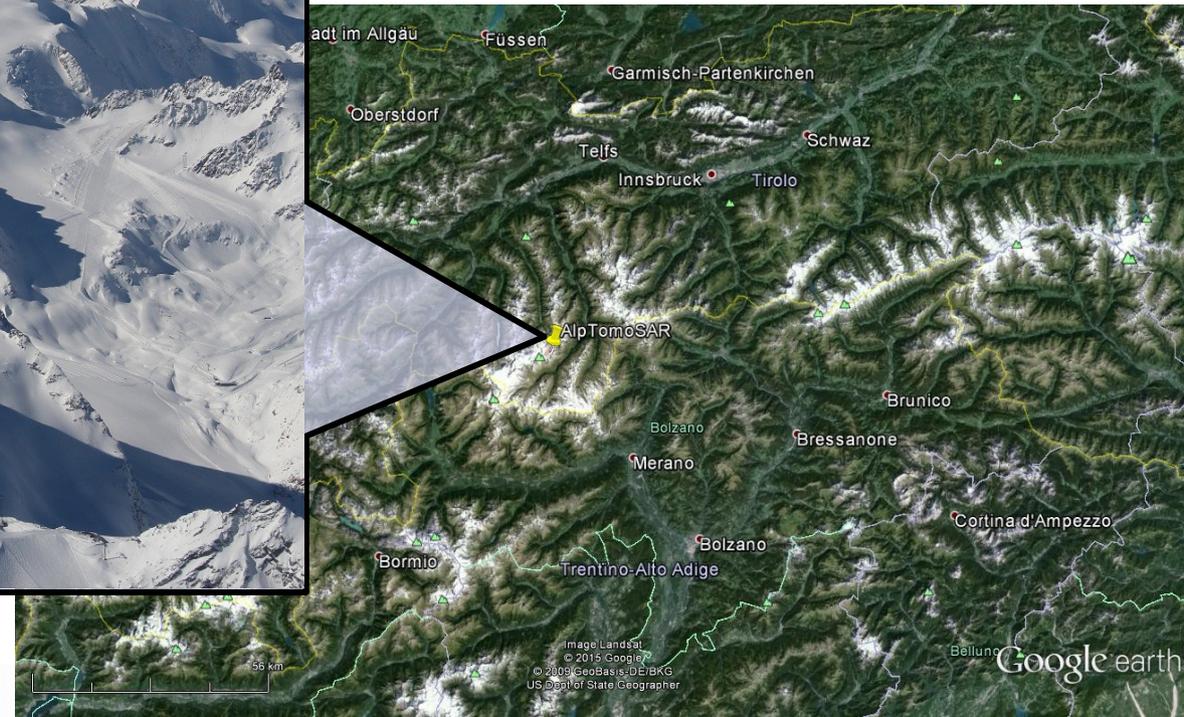
0 Weaker air/snow and stronger snow/ice and ice/seawater scattering at HV than at VV

⇒ Mostly polarized contributions from regular spherical snow grains

⇒ Depolarized contributions from irregular air bubbles in the ice layer

## **Test site:** Mittelbergferner, Austrian Alps

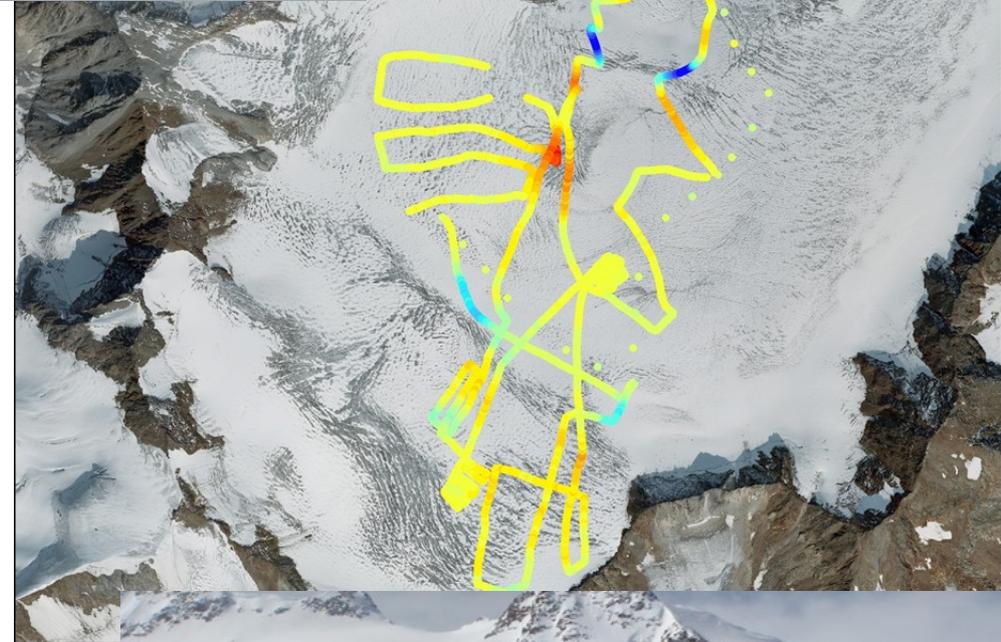
- temperate glacier at the main ridge of the Alps in Tyrol
- main test area is a flat plateau in the upper part of the glacier between 3000 and 3200 m



# Field Works

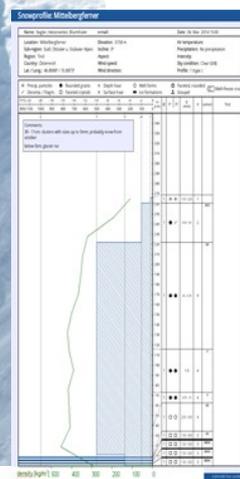
## Field activities

- Setting up Corner Reflectors
- Stratigraphy of winter snow pack
  - Density / Hardness, ice layers, grain size
- Transects of snow depth
- GPR Measurements



## GPR Equipment:

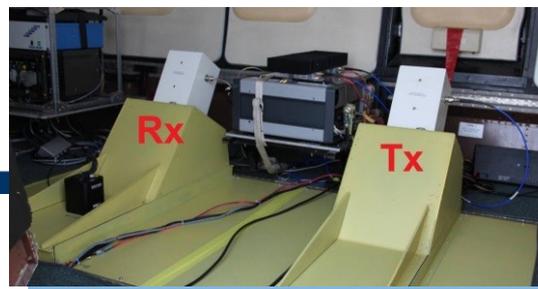
- IDS dual-frequency 200/600 MHz
- Total length of GPR profile: 18 km



# SAR Acquisitions

## SAR Equipment:

- FMCW SAR by MetaSensing
- Transmitted bandwidth: 150 MHz
- Central frequency: 1275 MHz
- Fully polarimetric
- Spatial resolution  $\leq 2 \times 2$  m (ground range, azimuth)



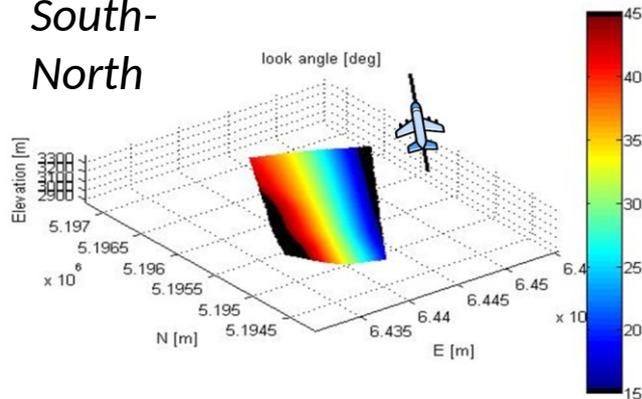
## Aircraft

- CASA C-212 operated by CGR

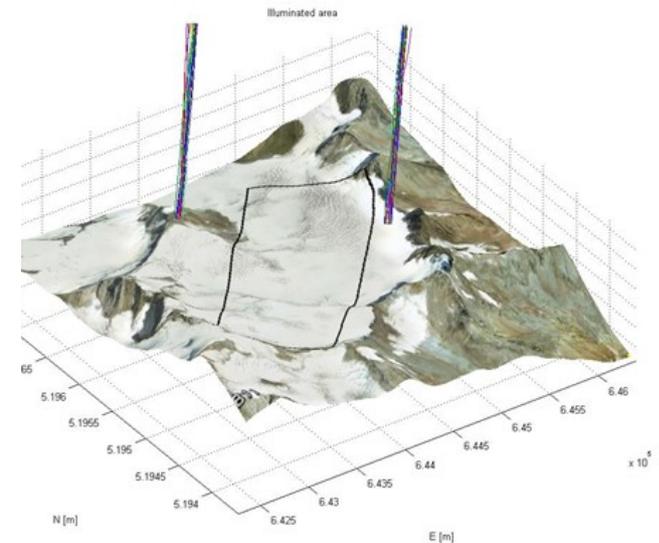
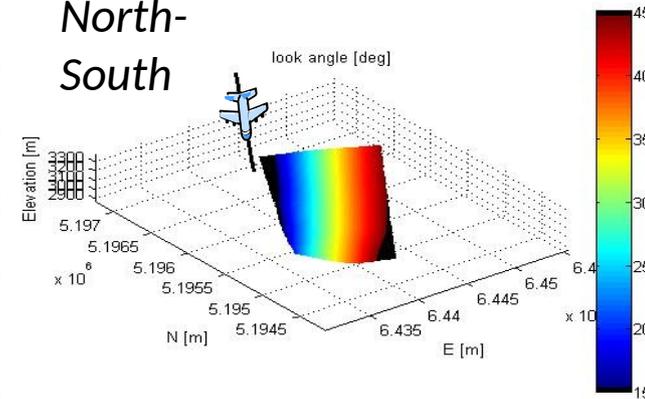
## Flights:

- Two flight directions
- 20+20 passes

## South-North

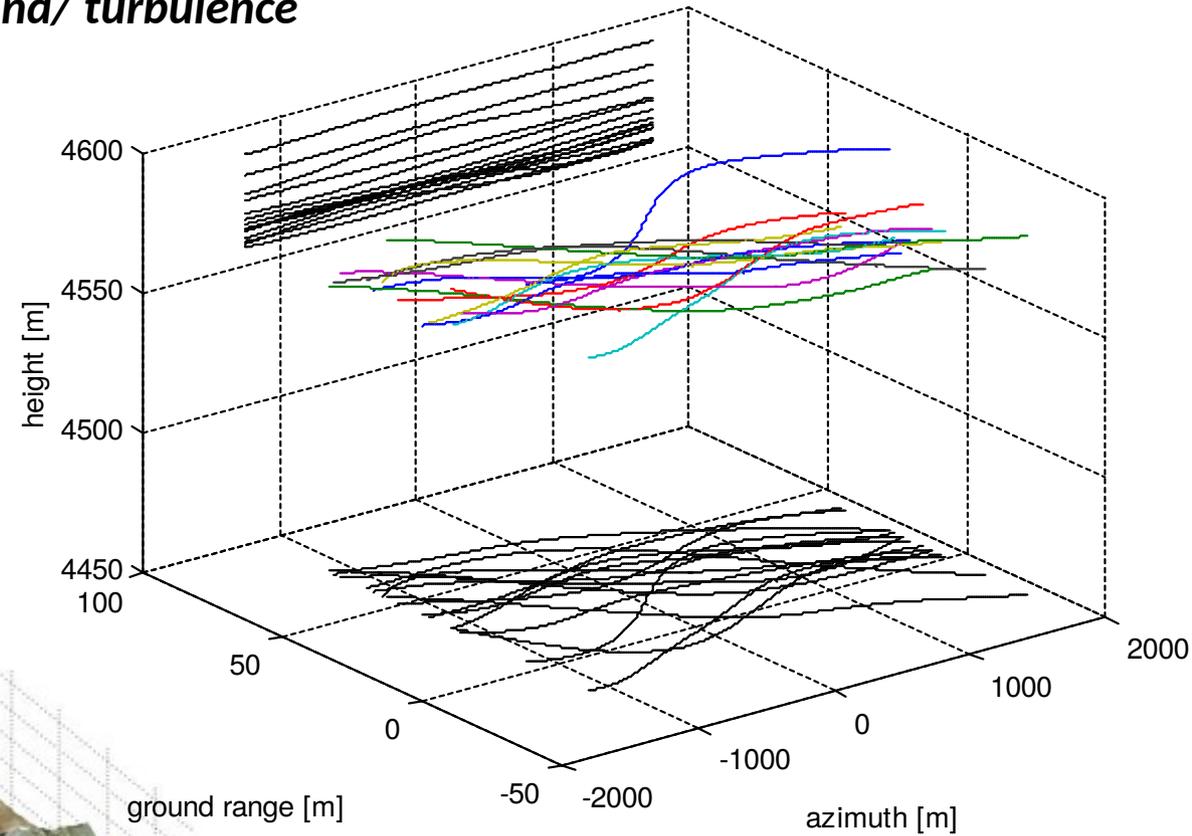
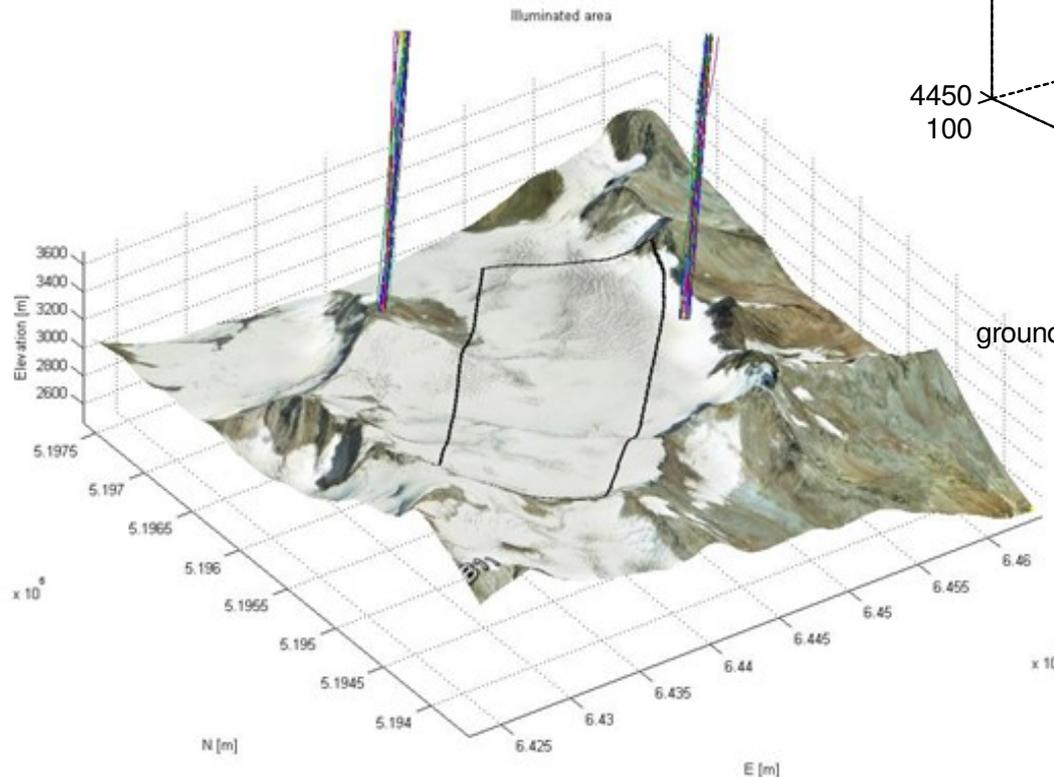


## North-South



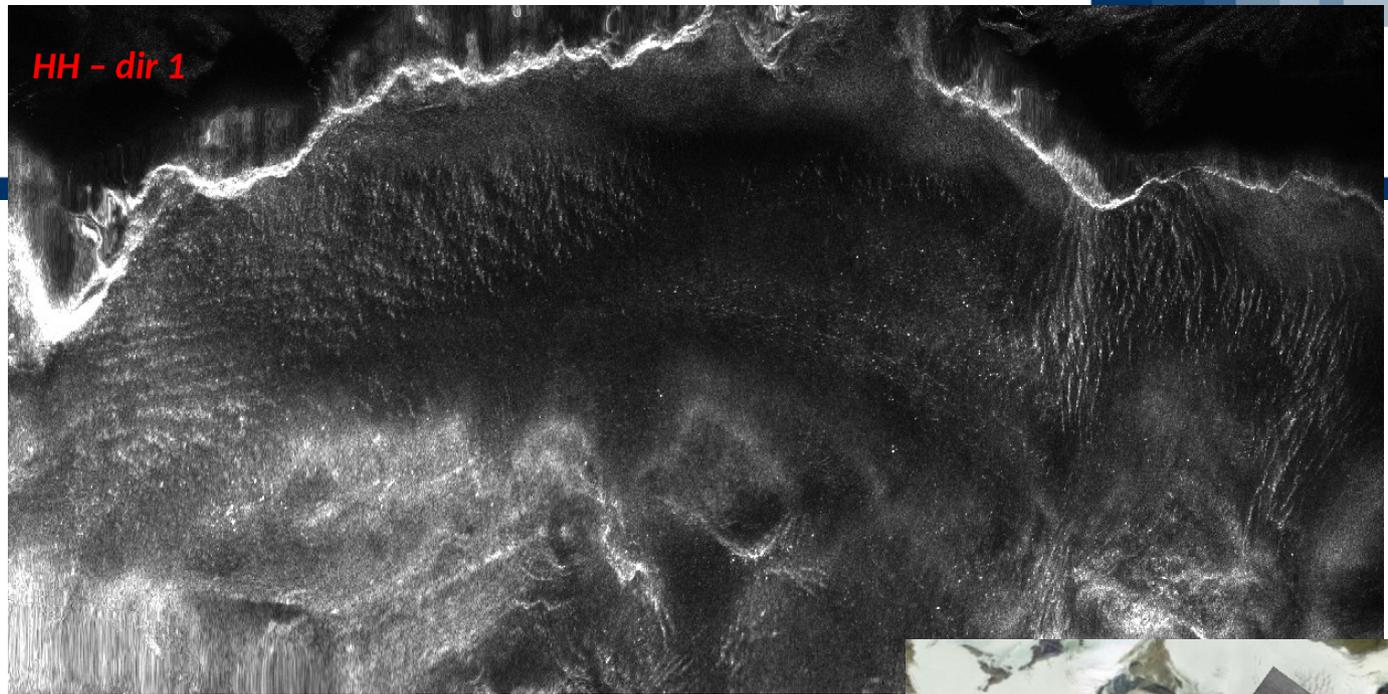
## *Strong trajectory perturbation caused by wind/ turbulence*

- 0 Max along track variation > 50 m
- 0 No auto-piloting system
- 0 Proximity to mountain peaks



# 2D Focusing

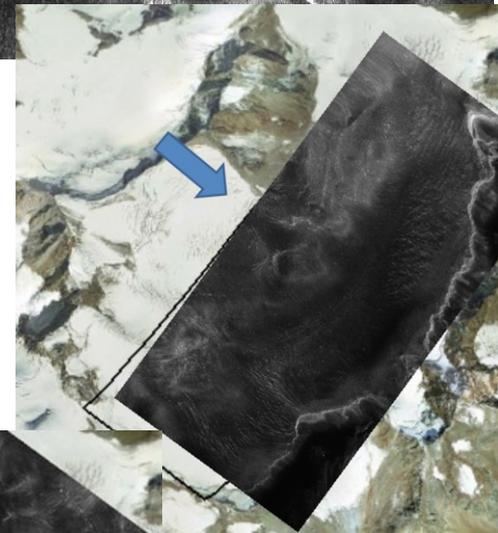
*HH - dir 1*



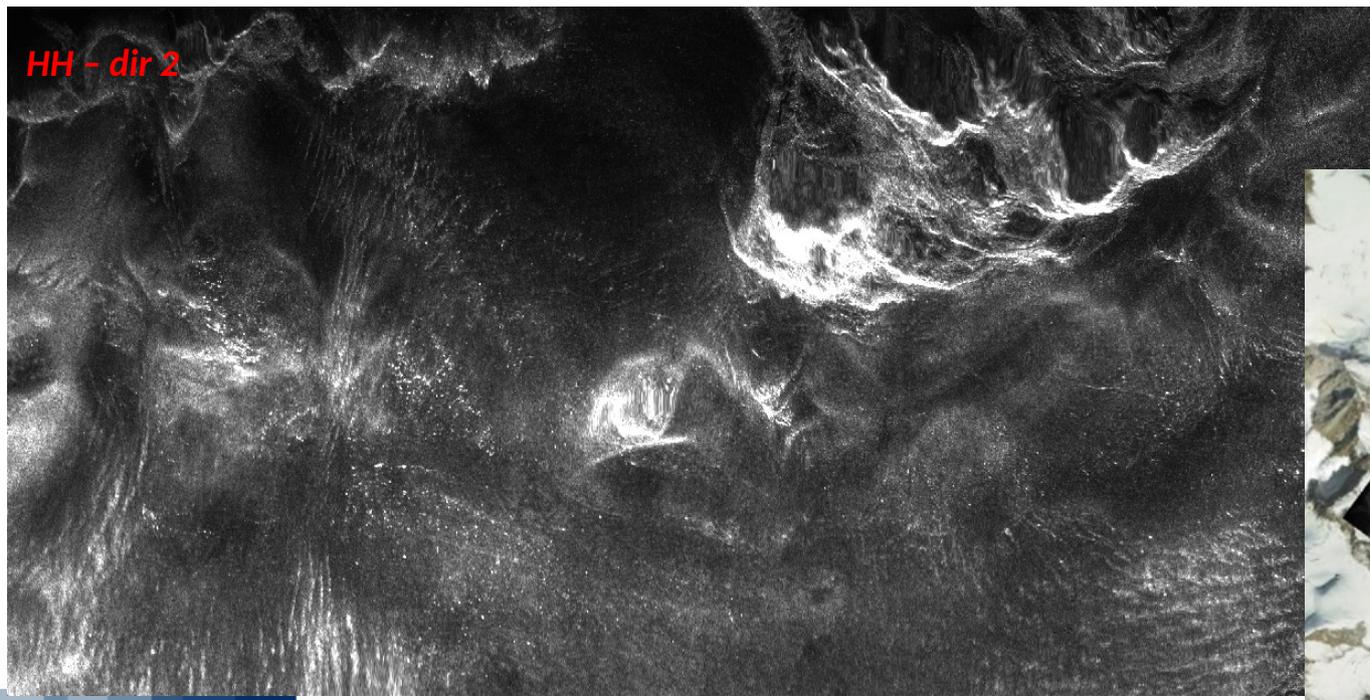
## 2D Focusing via Time Domain Back

### Projection on a reference DEM

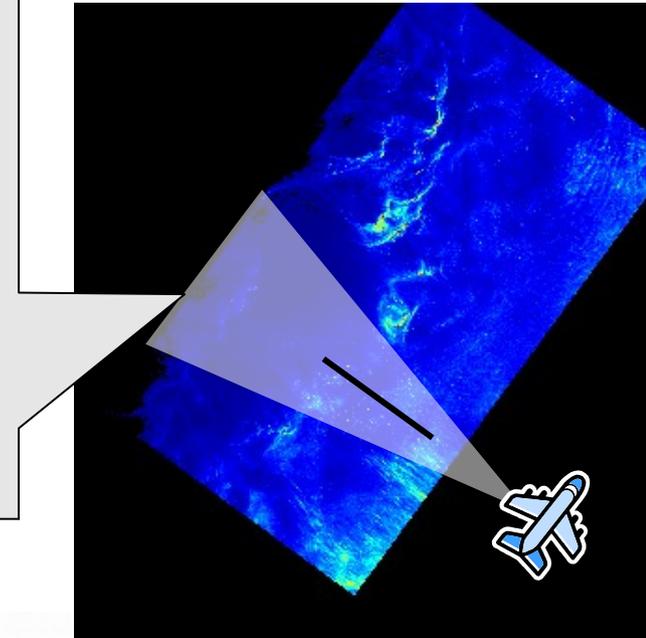
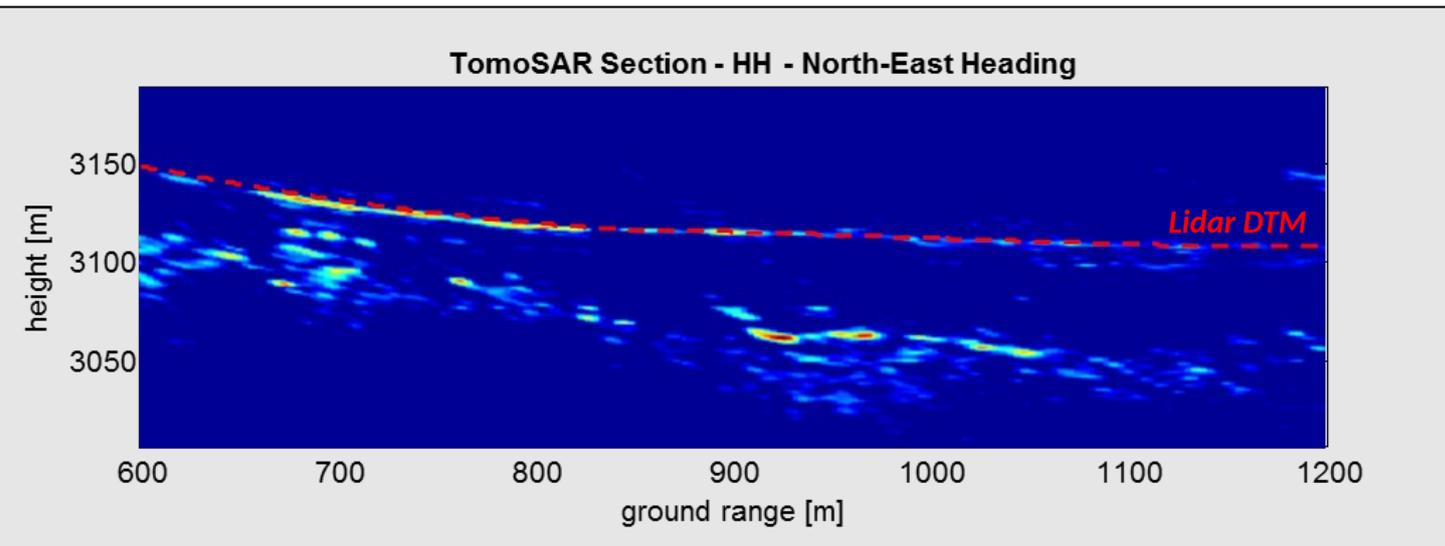
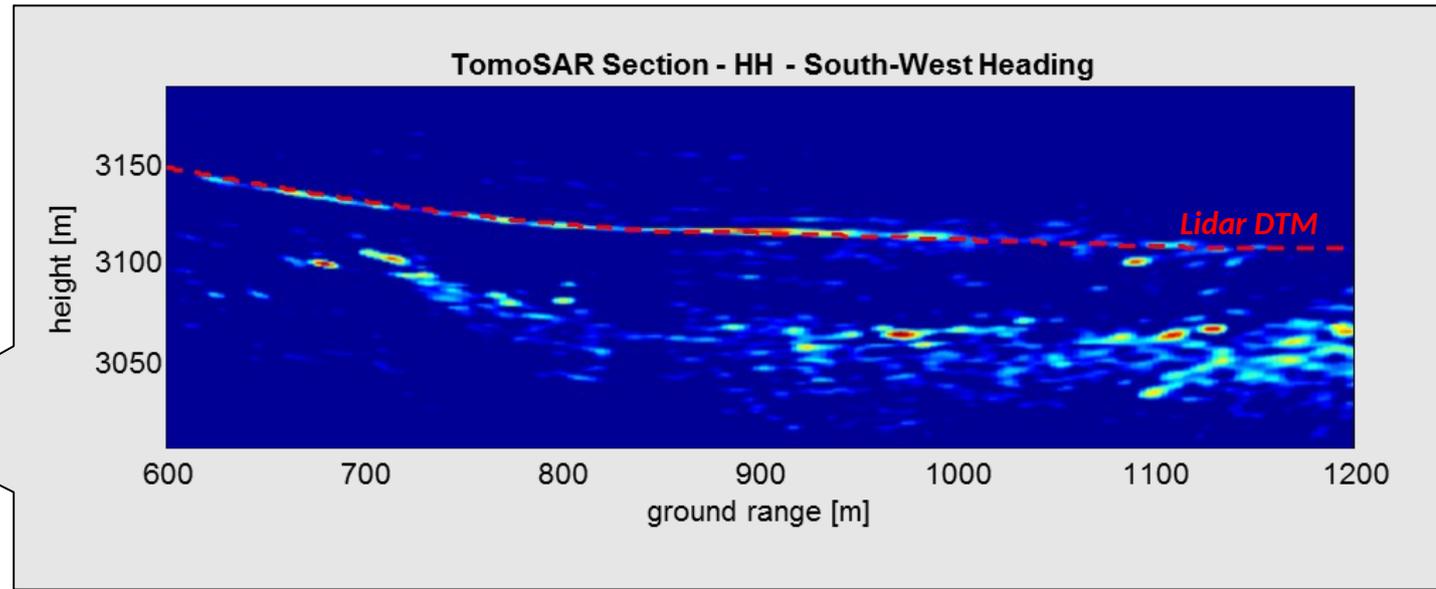
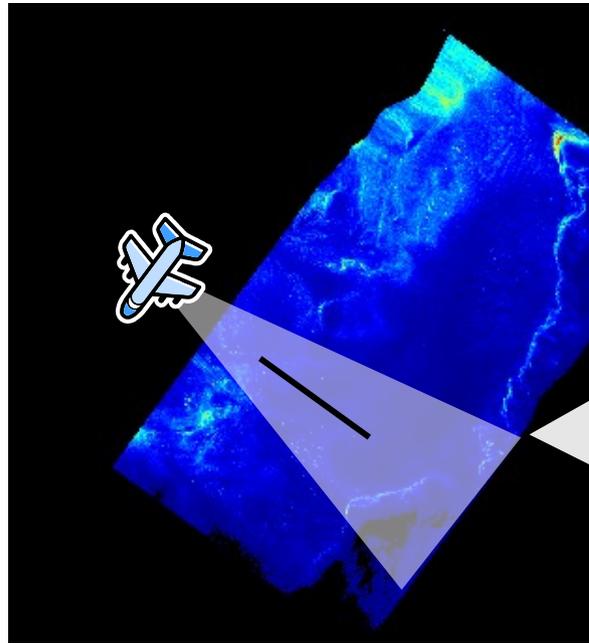
- 0 Optimal motion compensation
- 0 Common target wavenumbers in all passes
- 0 Automatic coregistration at the reference elevation



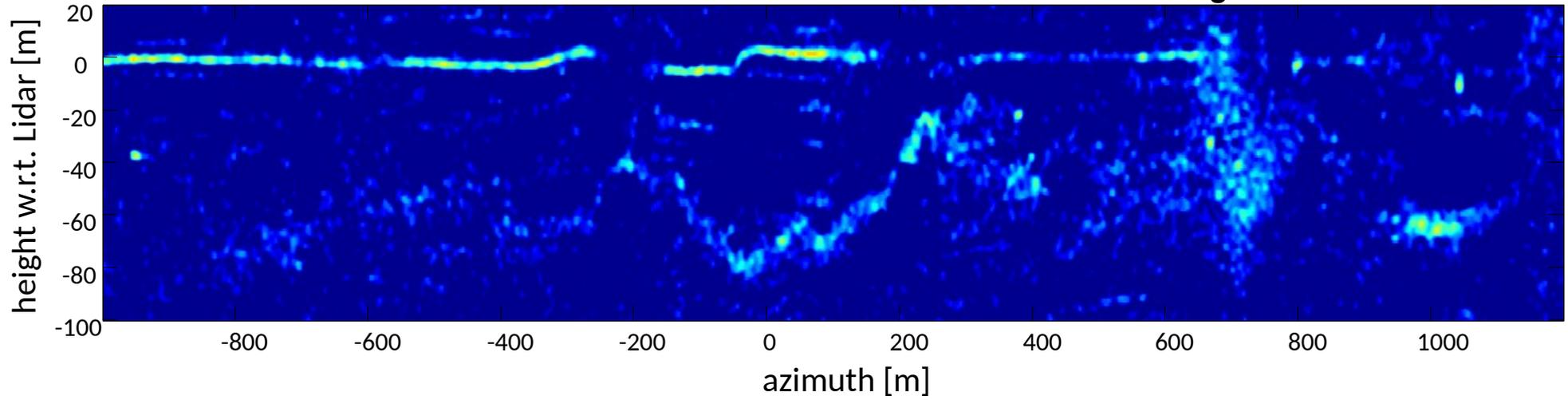
*HH - dir 2*



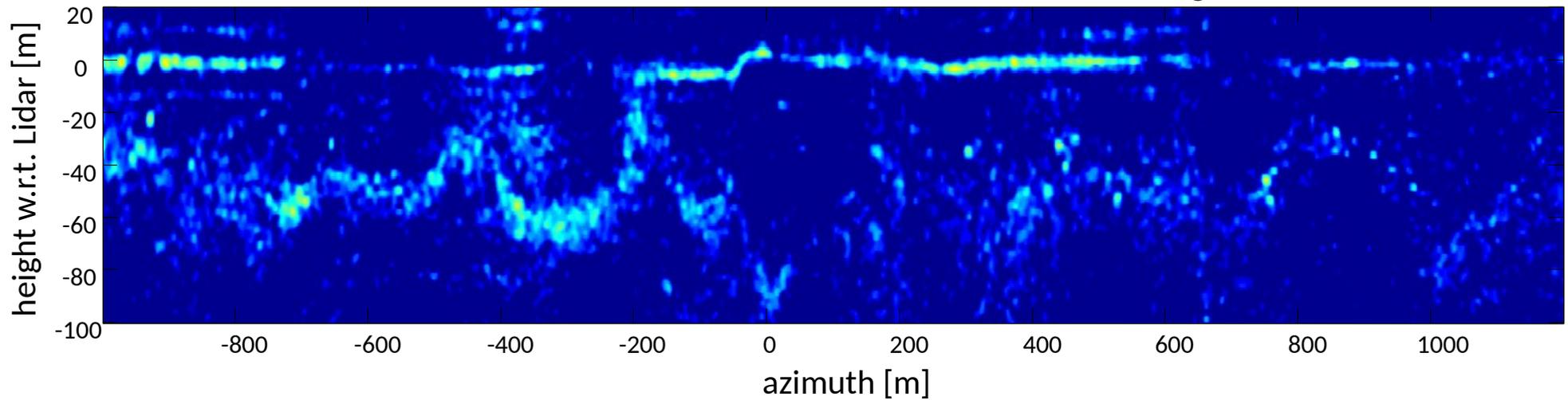
# 3D Focusing



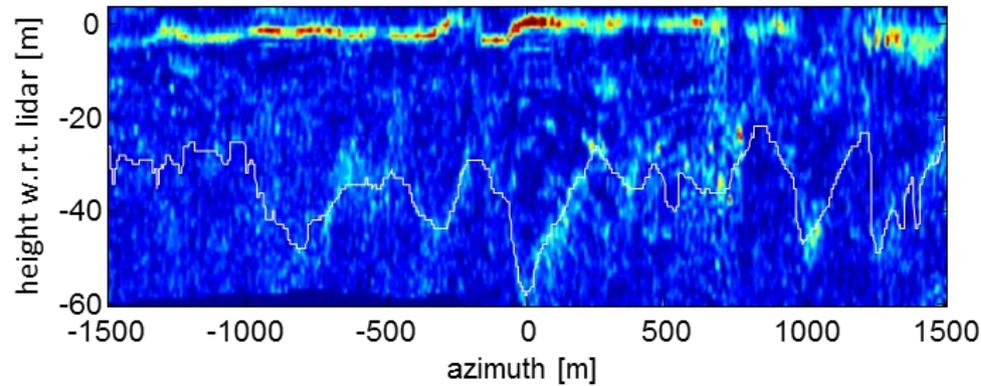
**TomoSAR Vertical Section - HH - South-West Heading**



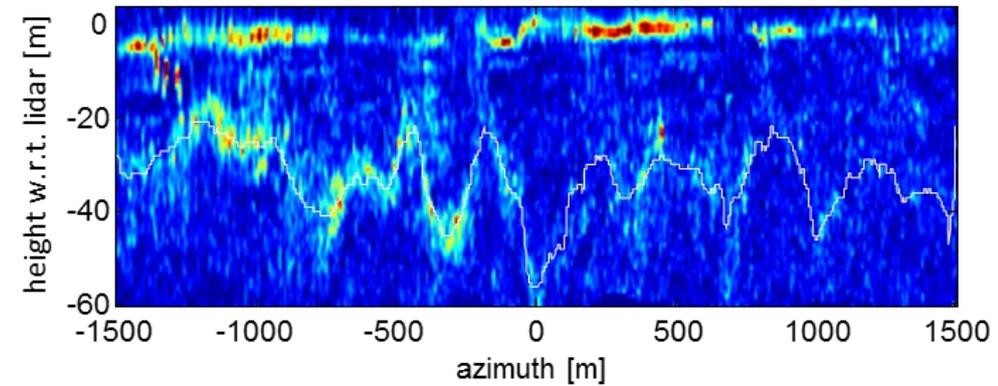
**TomoSAR Vertical Section - HH - North-East Heading**



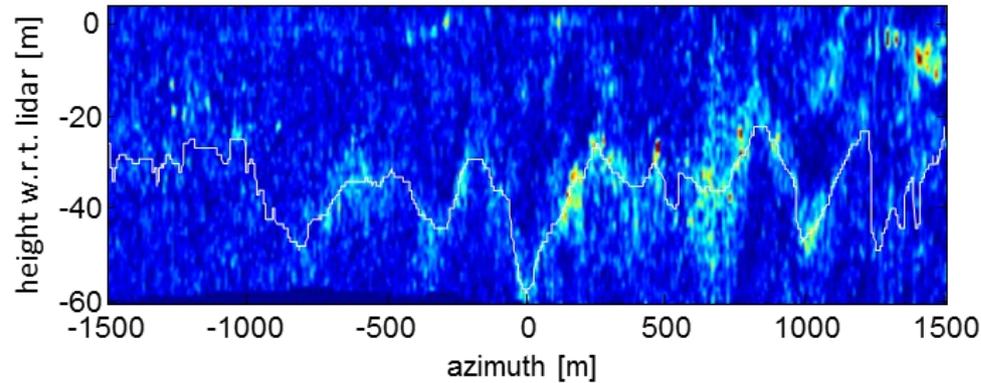
TomoSAR section - HH - Direction 1



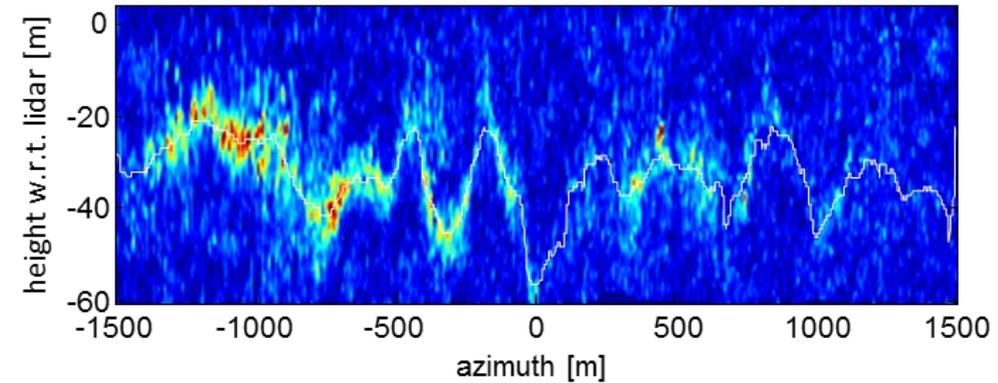
TomoSAR section - HH - Direction 2



TomoSAR section - HV - Direction 1



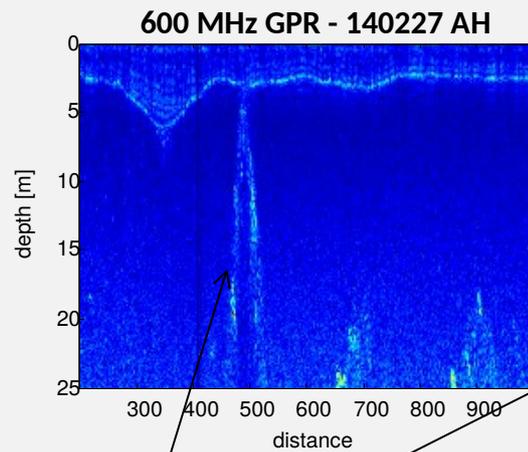
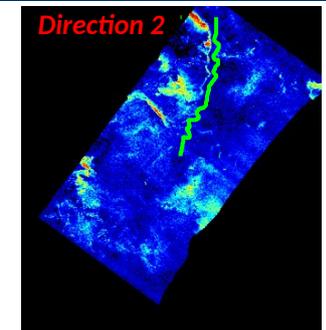
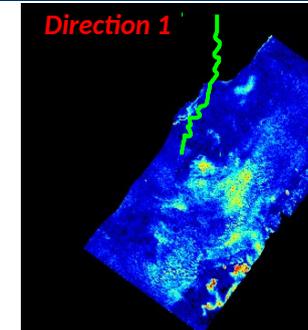
TomoSAR section - HV - Direction 2



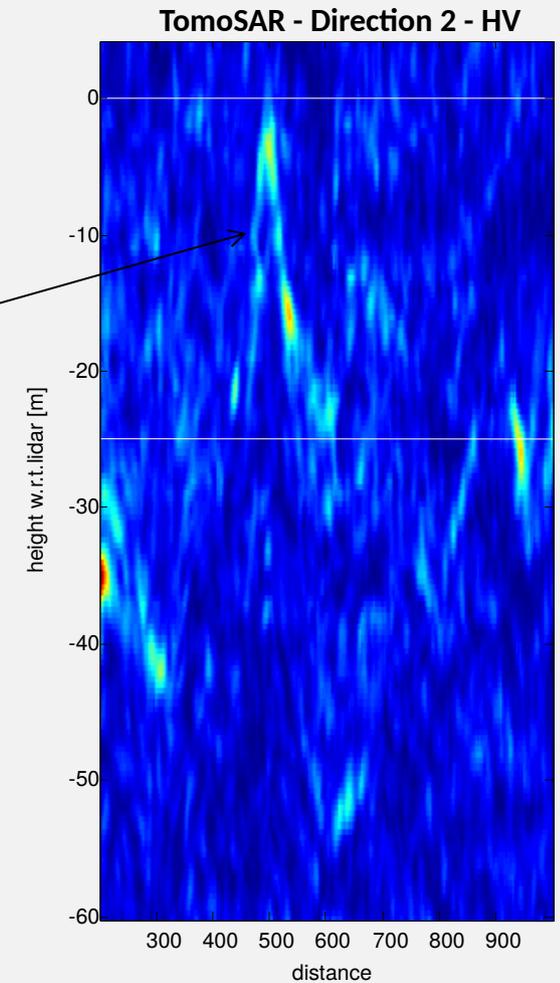
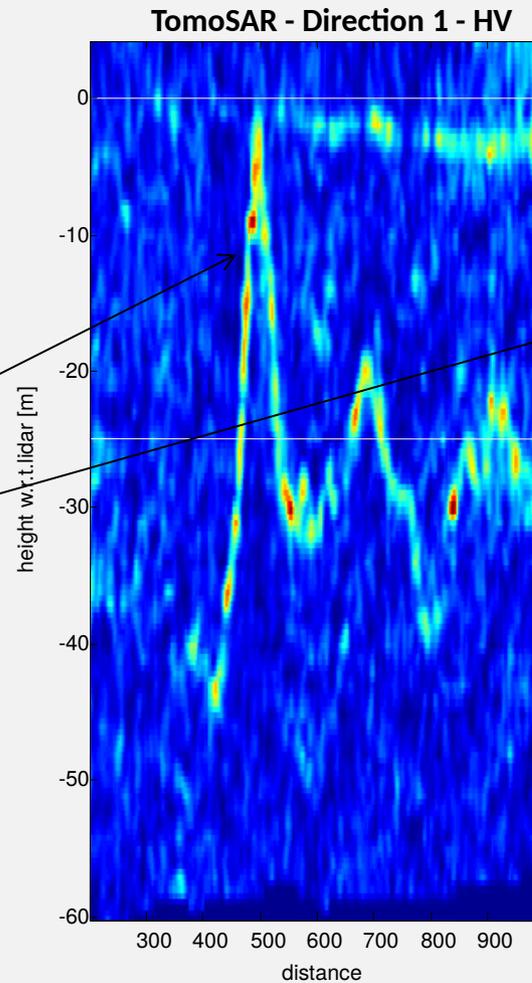
- 0 Clear signal from the ice/snow interface in co-polarized channels
- 0 Clear signal from down to 60 m beneath in all polarizations

# Comparison to 600 MHz GPR Transects

- TomoSAR vs GPR comparison by sampling TomoSAR cubes along GPR transects
- 600 MHz GPR transects processed down to 25 m
- TomoSAR transects processed down to 60 m

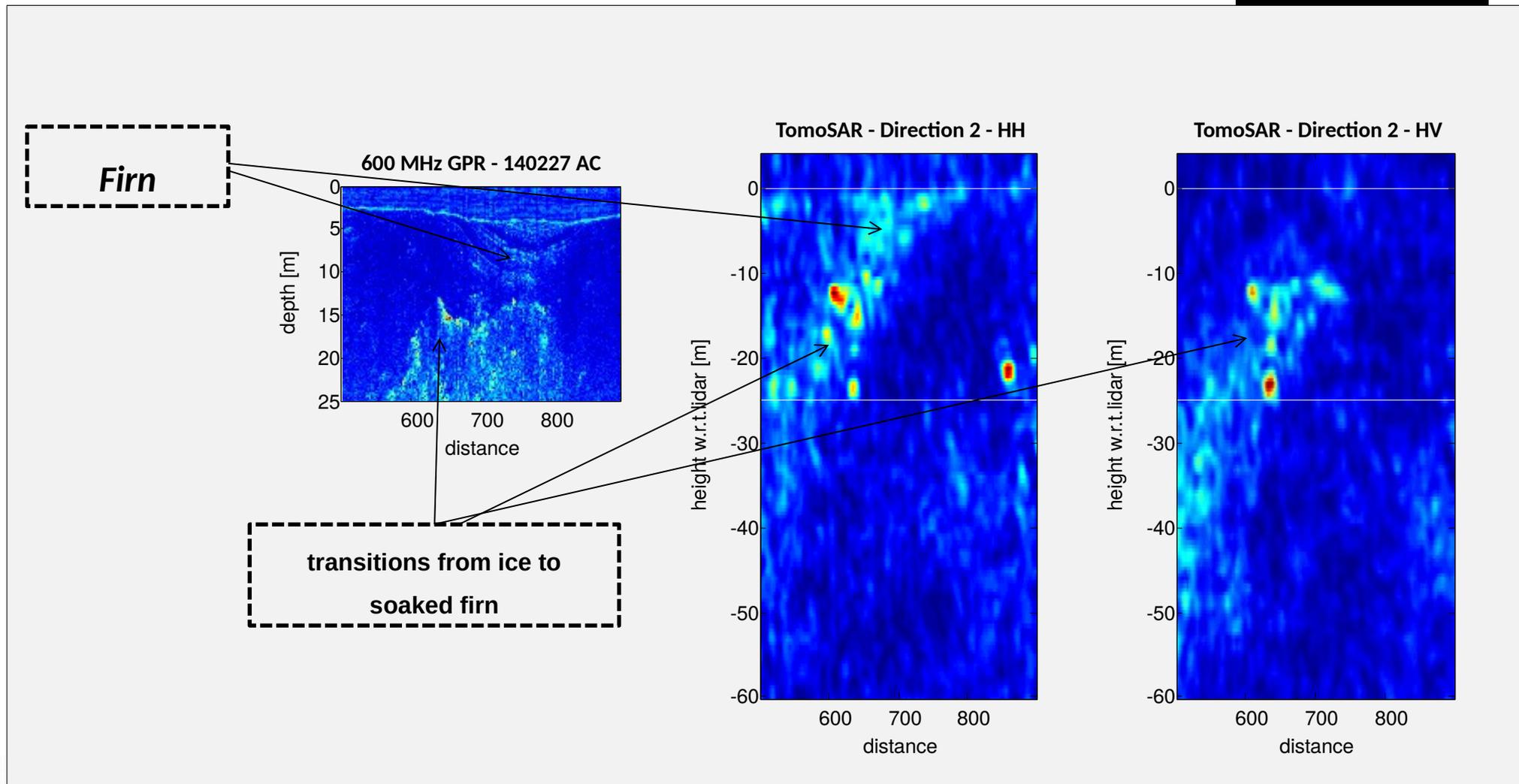
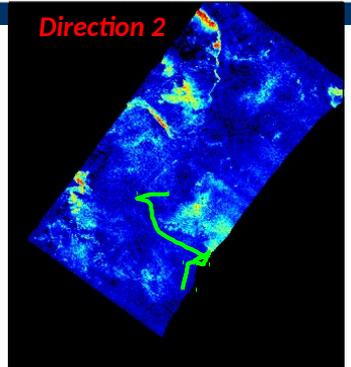


**Bedrock**

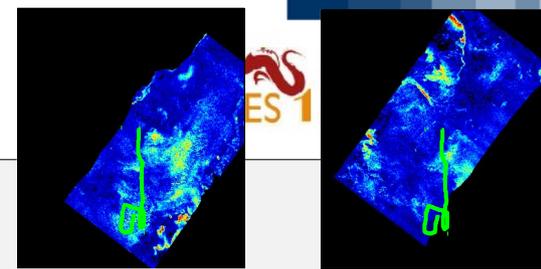


# Comparison to 600 MHz GPR Transects

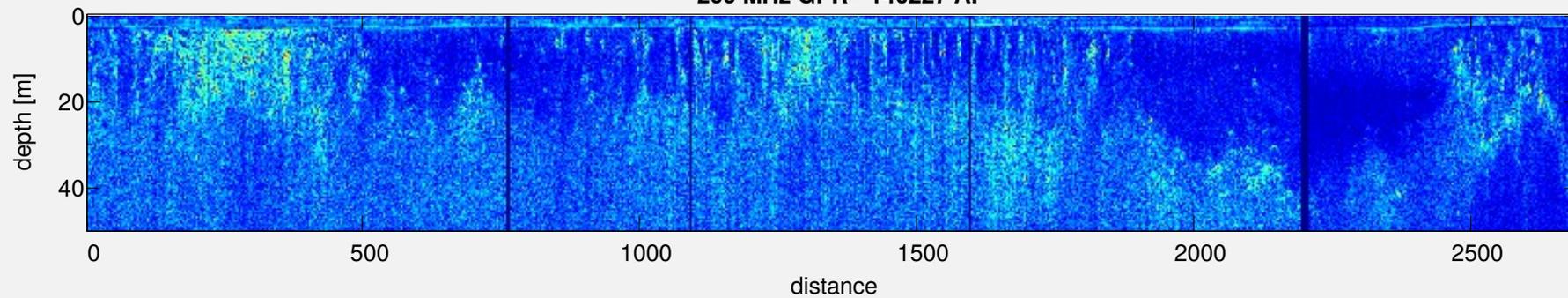
- TomoSAR vs GPR comparison by sampling TomoSAR cubes along GPR transects
- 600 MHz GPR transects processed down to 25 m
- TomoSAR transects processed down to 60 m



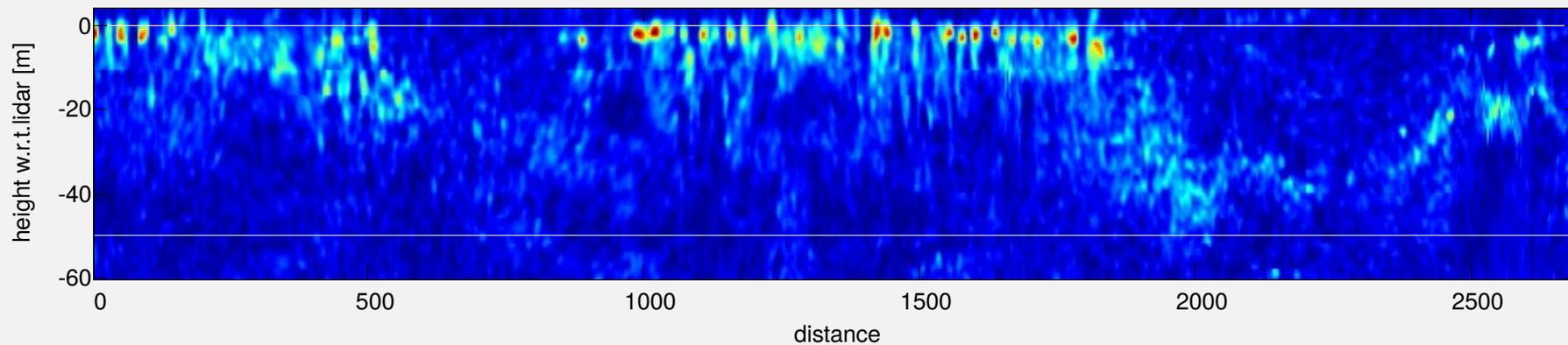
# Comparison to 200 MHz GPR Transects



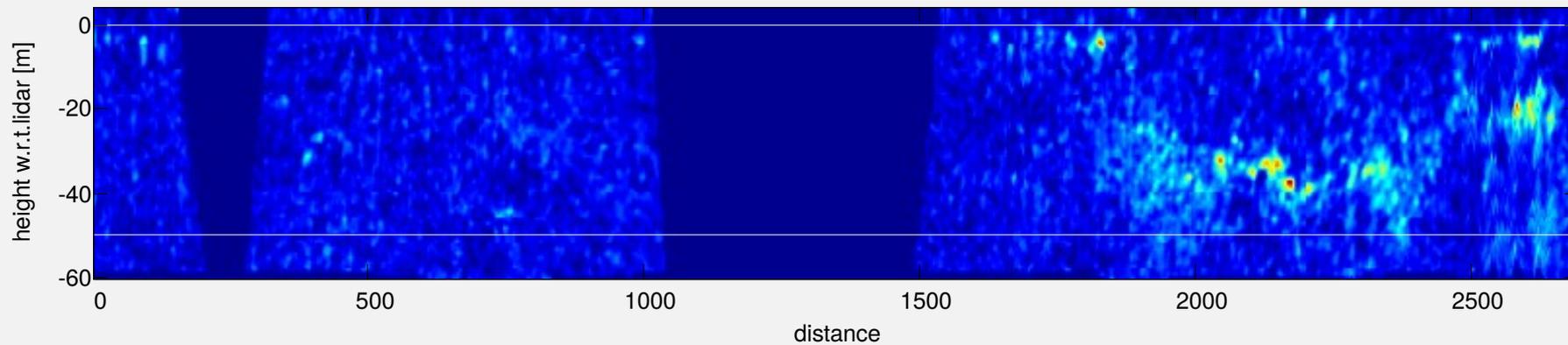
200 MHz GPR - 140227 AF



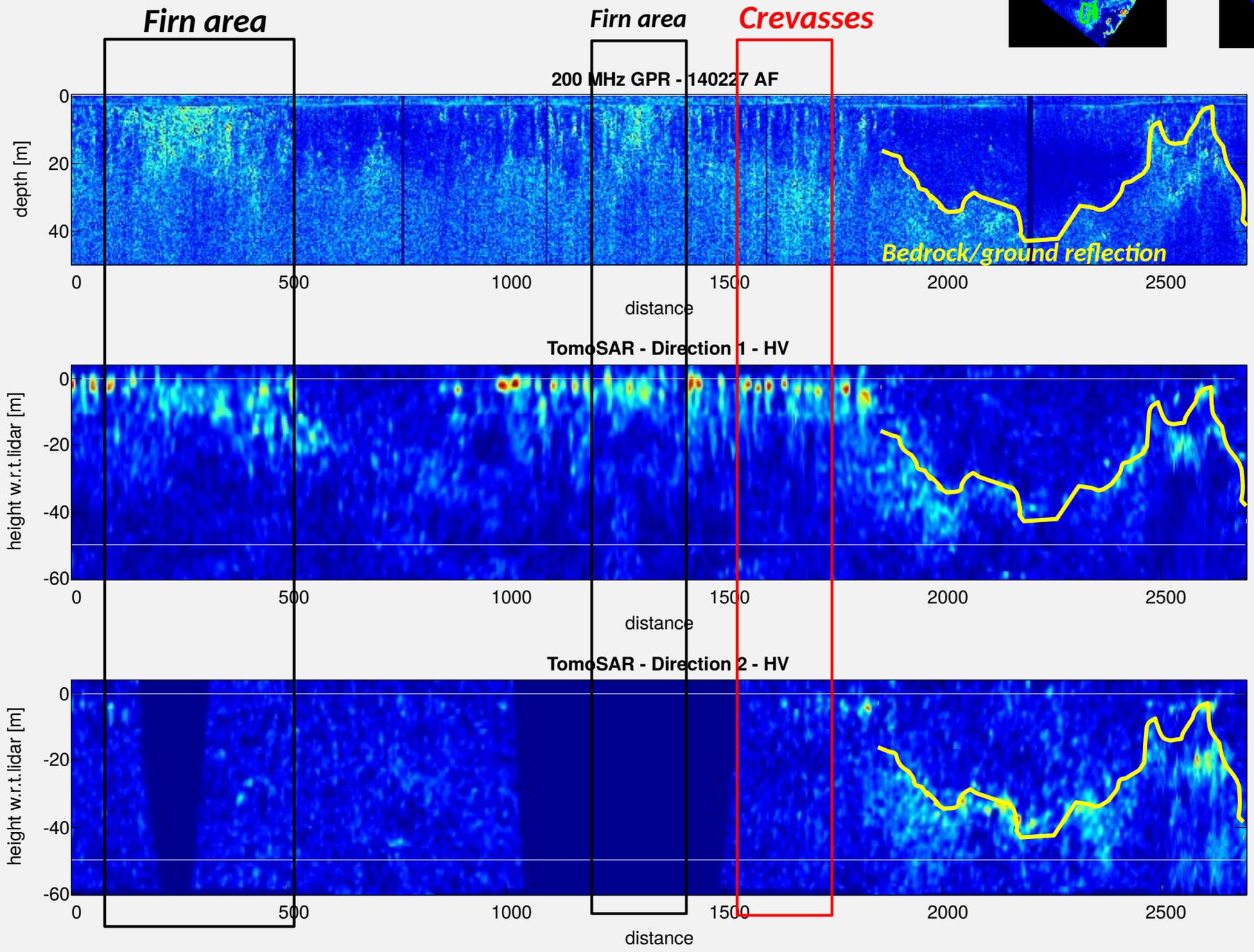
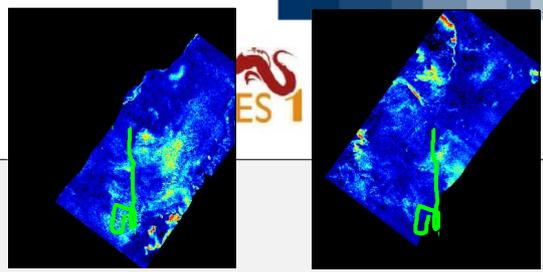
TomoSAR - Direction 1 - HV



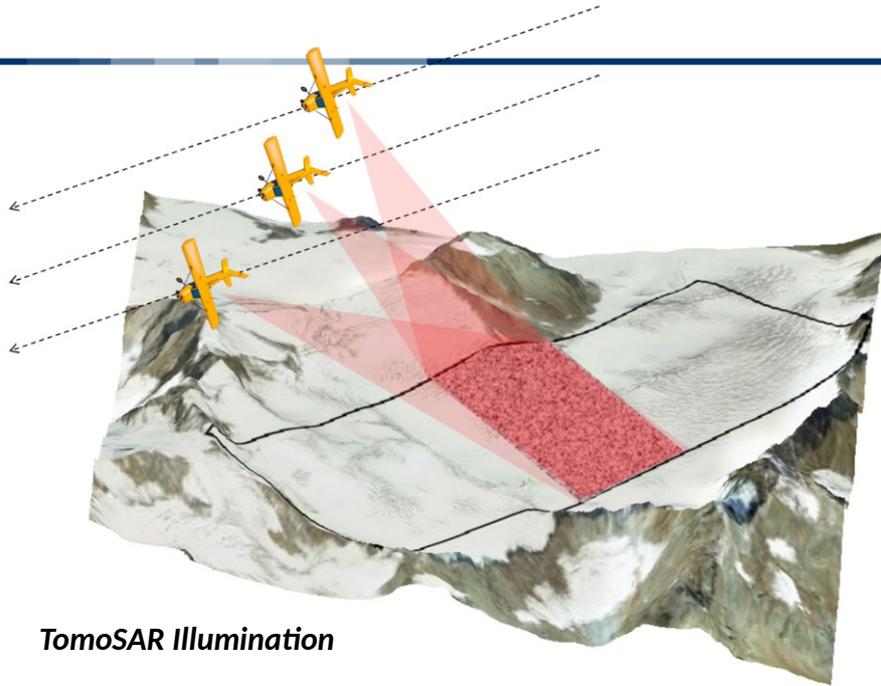
TomoSAR - Direction 2 - HV



# Comparison to 200 MHz GPR Transects

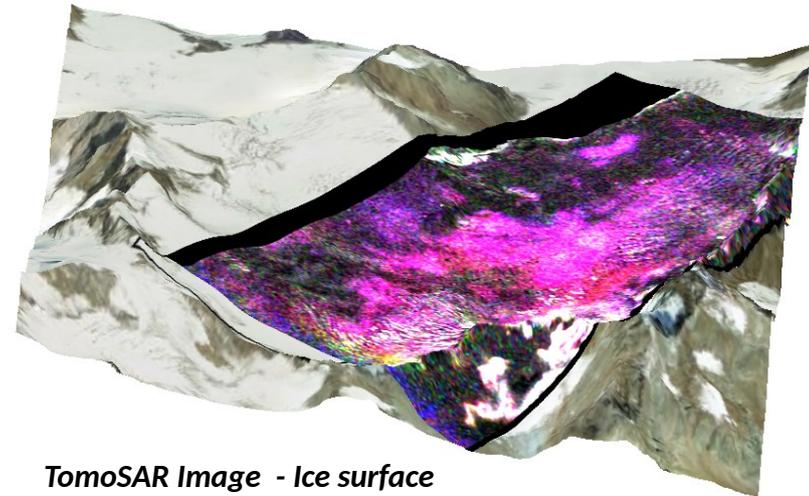


# 3D Polarimetry

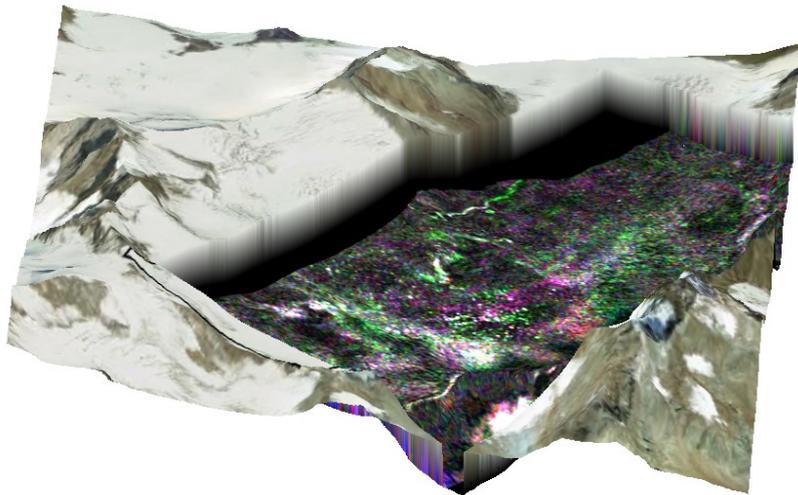


*TomoSAR Illumination*

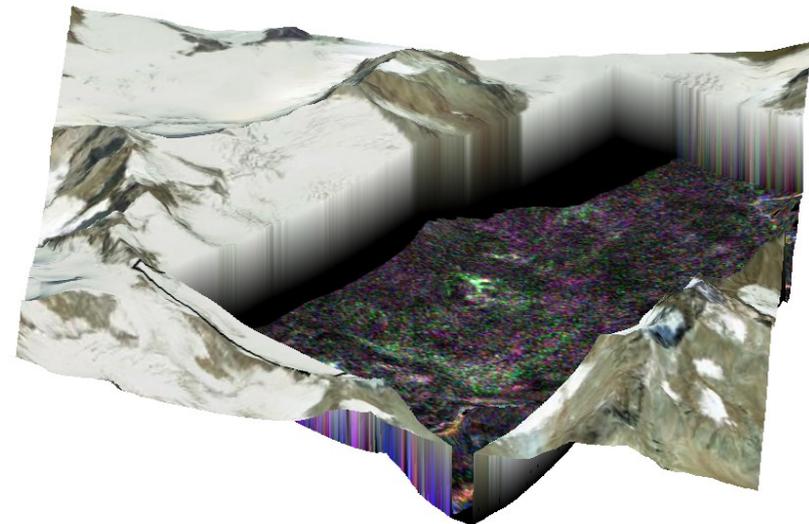
(normalized) HH - red  
(normalized) HV - green  
(normalized) VV - blue



*TomoSAR Image - Ice surface*



*TomoSAR Image - 25 m below the Ice surface*



*TomoSAR Image - 50 m below the Ice surface*